

List of Boundary-value Problem (P2C) for 2D Cartesian Domains, for which the Green's Functions for Poisson's Equation have been derived

All these Green's functions can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

(P2C) 1. **Plane** ($-\infty \leq x_1, x_2 \leq \infty$)

In this section formulates boundary-value Problem (P2C)s on constructing Green's functions G of Poisson equation for the plane

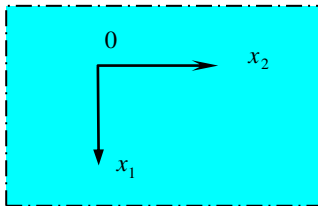


Figure 1: Plane in Cartesian co-ordinates.

Boundary-value Problem (P2C)

Let us consider the following boundary value Problem (P2C)s which consist from the Poisson equation

$$\begin{aligned}\nabla^2 G(x_1, \xi_1; x_2, \xi_2) &= -\delta(x - \xi); \\ \nabla^2 U(x_1, x_2) &= -f(x_1, x_2).\end{aligned}$$

in the inner points of the plane. At infinity the functions G and U must vanish.

The Answer to the **Problem (P2C)** 1.1 for plane can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

(P2C) 2. Half-plane ($0 \leq x_1 \leq \infty, -\infty \leq x_2 \leq \infty$)

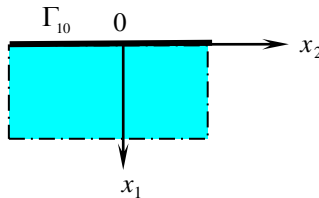


Figure 2: Half-plane with the boundary straight line Γ_{10} .

(P2C) Boundary-value Problems

Let us consider the following boundary value Problem (P2C)s which consist from the Poisson equation

$$\begin{aligned} \nabla^2 G(x_1, \xi_1; x_2, \xi_2) &= -\delta(x - \xi); \\ \nabla^2 U(x_1, x_2) &= -f(x_1, x_2) \end{aligned}$$

in the inner points of the half-plane. On its boundaries are given the following boundary conditions:

Problem (P2C) 2.1

$$G^{(1)}(x, \xi) = 0; x_1 = 0; -\infty \leq x_2 \leq \infty; U(0, y_2) = s(0, y_2)$$

The Answer to Problem (P2C) 2.1 for half-plane (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 2.2

$$\frac{\partial}{\partial x_1} G^{(2)} = 0; x_1 = 0; -\infty \leq x_2 \leq \infty;$$
$$\partial U(0, y_2) / \partial n_1 = g(0, y_2)$$

The Answer to Problem (P2C) 2.2 for half-plane (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

(P2C) 3. Quadrant ($0 \leq x_1, x_2 \leq \infty$)

In this section formulates four boundary-value Problems (P2C) on constructing Green's functions, $G^{(j)}$, $j=1-4$, of Poisson's equation for the quadrant

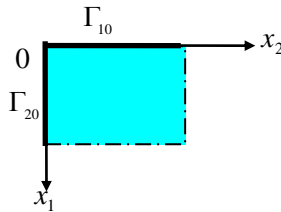


Figure 3: Quadrant with boundary half-straight lines Γ_{10} and Γ_{20} .

(P2C) 3.1. Boundary-value Problems and integral representation via Green's functions

Let us consider the following boundary value Problem (P2C)s which consist from the Poisson equation

$$\nabla^2 U(x_1, x_2) = -f(x_1, x_2) \tag{3.1}$$

in the inner points of the quadrant. On the boundaries are given two of the following four functions:

$$\begin{aligned} \partial U(0, y_2)/\partial n_1 &= g_1(0, y_2) \text{ or } U(0, y_2) = s_1(0, y_2); \\ \partial U(y_1, 0)/\partial n_2 &= g_2(y_1, 0) \text{ or } U(y_1, 0) = s_2(y_1, 0). \end{aligned} \quad (3.2)$$

The solutions of these boundary value Problem (P2C)s are expressed via respective Green functions in the form of following integral formula:

$$\begin{aligned} U(x_1, x_2) &= \int_0^\infty \int_0^\infty f(\xi_1, \xi_2) G(x_1, \xi_1; x_2, \xi_2) d\xi_1 d\xi_2 + \\ &\int_0^\infty \left[\frac{\partial U(0, y_2)}{\partial n_1} G(0, x_1; y_2, x_2) - U(0, y_2) \frac{\partial G(0, x_1; y_2, x_2)}{\partial n_1} \right] dy_2 + \\ &\int_0^\infty \left[\frac{\partial U(y_1, 0)}{\partial n_2} G(y_1, x_1; 0, x_2) - U(y_1, 0) \frac{\partial G(y_1, x_1; 0, x_2)}{\partial n_2} \right] dy_1. \end{aligned} \quad (3.3)$$

In eq. (3.3) Green functions G and functions U satisfy Poisson equations

$$\begin{aligned} \nabla^2 G(x_1, \xi_1; x_2, \xi_2) &= -\delta(x - \xi); \\ \nabla^2 U(x_1, x_2) &= -f(x_1, x_2) \end{aligned} \quad (3.4)$$

and the following boundary conditions:

Problems (P2C) 3.1- (P2C) 3.4

And construct the Green's function $G^{(j)}(x, \xi)$, $j=1-4$ for Poisson's equation $\nabla^2 G(x, \xi) = -\delta(x - \xi)$ for the quadrant ($0 \leq x_1 \leq \infty$, $0 \leq x_2 \leq \infty$) under the following homogeneous boundary conditions

Problem (P2C) 3.1

$\begin{aligned} G^{(1)} &= 0; x_1 = 0, 0 \leq x_2 \leq \infty; U(0, y_2) = s_1(0, y_2); \\ G^{(1)} &= 0; x_2 = 0, 0 \leq x_1 \leq \infty; U(y_1, 0) = s_2(y_1, 0). \end{aligned}$
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The Answer to Problem (P2C) 3.1 for quadrant (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).

2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 3.2

$$\frac{\partial \mathcal{G}^{(2)}}{\partial x_1} = 0; \quad x_1 = 0, 0 \leq x_2 \leq \infty; \quad \partial U(0, y_2) / \partial n_1 = g_1(0, y_2);$$

$$\frac{\partial \mathcal{G}^{(2)}}{\partial x_2} = 0; \quad x_2 = 0, 0 \leq x_1 \leq \infty; \quad \partial U(y_1, 0) / \partial n_2 = g_2(y_1, 0).$$

The Answer to **Problem (P2C) 3.2 for quadrant** (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 3.3

$$G^{(3)} = 0; \quad x_1 = 0, 0 \leq x_2 \leq \infty; \quad U(0, y_2) = s_1(0, y_2);$$

$$\frac{\partial G^{(3)}}{\partial x_2} = 0; \quad x_2 = 0, 0 \leq x_1 \leq \infty; \quad \partial U(y_1, 0) / \partial n_2 = g_2(y_1, 0).$$

The Answer to **Problem (P2C) 3.3 for quadrant** (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 3.4

$$\frac{\partial G^{(4)}}{\partial x_1} = 0; \quad x_1 = 0, 0 \leq x_2 \leq \infty; \quad \partial U(0, y_2) / \partial n_1 = g_1(0, y_2);$$
$$G^{(4)} = 0; \quad x_2 = 0, 0 \leq x_1 \leq \infty; \quad U(y_1, 0) = s_2(y_1, 0)$$

The Answer to Problem (P2C) 3.4 for quadrant (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

(P2C) 4. Strip ($-\infty \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2$)

In this Section for boundary-value Problem (P2C)s on constructing Green's function $G^{(j)}$, ($j=1-4$) of Poisson's equation for a strip are formulated

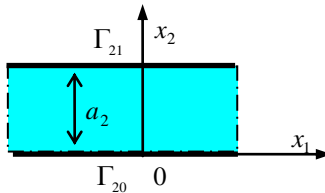


Figure 4: Strip with boundary straight lines Γ_{20} and Γ_{21} .

(P2C) 4.1. Boundary-value Problems and integral representation via Green's functions

Let us consider the following boundary value Problem (P2C)s which consist from the Poisson equation

$$\nabla^2 U(x_1, x_2) = -f(x_1, x_2) \tag{4.1}$$

in the inner points of the quadrant. On the boundaries are given two of the following four functions:

$$\begin{aligned} \partial U(y_1, 0) / \partial n_2 &= g_1(y_1, 0) \text{ or } U(y_1, 0) = s_1(y_1, 0); \\ \partial U(y_1, a_2) / \partial n_2 &= g_2(y_1, a_2) \text{ or } U(y_1, a_2) = s_2(y_1, a_2). \end{aligned} \quad (4.2)$$

The solutions of these boundary value Problem (P2C)s are expressed via respective Green functions in the form of following integral formula:

$$\begin{aligned} U(x_1, x_2) &= \int_{-\infty}^{\infty} \int_0^{\infty} f(\xi_1, \xi_2) G(x_1, \xi_1; x_2, \xi_2) d\xi_1 d\xi_2 + \\ &\int_{-\infty}^{\infty} \left[\frac{\partial U(y_1, 0)}{\partial n_2} G(y_1, x_1; 0, x_2) - U(y_1, 0) \frac{\partial G(y_1, x_1; 0, x_2)}{\partial n_2} \right] dy_1 + \\ &\int_{-\infty}^{\infty} \left[\frac{\partial U(y_1, a_2)}{\partial n_2} G(y_1, x_1; a_2, x_2) - U(0, y_2) \frac{\partial G(y_1, x_1; a_2, x_2)}{\partial n_2} \right] dy_1 \end{aligned} \quad (4.3)$$

In eq. (4.3) Green functions G and functions U satisfy Poisson equations

$$\begin{aligned} \nabla^2 G(x_1, \xi_1; x_2, \xi_2) &= -\delta(x - \xi); \\ \nabla^2 U(x_1, x_2) &= -f(x_1, x_2) \end{aligned} \quad (4.4)$$

and the following boundary conditions:

Problems (P2C) 4.1-(P2C) 4.4 with the answers

To construct the Green's function $G(x, \xi)$ for Poisson's equation $\nabla^2 G(x, \xi) = -\delta(x - \xi)$ for the strip $(-\infty \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2)$ under the following conditions

Problem (P2C) 4.1

$$\begin{aligned} G^{(1)} &= 0; x_2 = 0, -\infty \leq x_1 \leq \infty; U(y_1, 0) = s_1(y_1, 0); \\ G^{(1)} &= 0; x_2 = a_2 - \infty \leq x_1 \leq \infty; U(y_1, a_2) = s_2(y_1, a_2). \end{aligned}$$

The Answer to Problem (P2C) 4.1 for strip (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).

2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 4.2

$$\frac{\partial G^{(2)}}{\partial x_2} = 0; x_2 = 0, -\infty \leq x_1 \leq \infty; \partial U(y_1, 0) / \partial n_2 = g_1(y_1, 0)$$

$$\frac{\partial G^{(2)}}{\partial x_2} = 0; x_2 = a_2, -\infty \leq x_1 \leq \infty; \partial U(y_1, a_2) / \partial n_2 = g_2(y_1, a_2).$$

The Answer to Problem (P2C) 4.2 for strip (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 4.3

$$\frac{\partial G^{(3)}}{\partial x_2} = 0; x_2 = 0, -\infty \leq x_1 \leq \infty; \partial U(y_1, 0) / \partial n_2 = g_1(y_1, 0)$$

$$G^{(3)} = 0; x_2 = a_2, -\infty \leq x_1 \leq \infty; U(y_1, a_2) = s_2(y_1, a_2).$$

The Answer to Problem (P2C) 4.3 for strip (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 4.4

$$G^{(4)} = 0; x_2 = 0, -\infty \leq x_1 \leq \infty; U(y_1, 0) = s_1(y_1, 0);$$

$$\frac{\partial G^{(4)}}{\partial x_2} = 0; x_2 = a_2, -\infty \leq x_1 \leq \infty; \partial U(y_1, a_2) / \partial n_2 = g_2(y_1, a_2).$$

The Answer to Problem (P2C) 4.4 for strip (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

(P2C) 5. Half-strip ($0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2$)

In this Section formulate eight boundary-value Problem (P2C)s on constructing Green's functions, $G^{(j)}$, ($j = 1-8$), of Poisson's equation for the half-strip

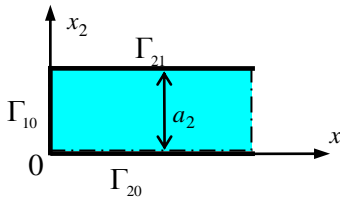


Figure 5: Half-strip with boundary half-straight lines Γ_{20} and Γ_{21} a segment of straight line Γ_{10} .

(P2C)5.1. Boundary-value Problems and integral representation via Green's functions

Let us consider the following boundary value Problem (P2C)s which consist from the Poisson equation

$$\nabla^2 U(x_1, x_2) = -f(x_1, x_2) \quad (5.1)$$

in the inner points of the quadrant. On the boundaries are given three of the following six functions:

$$\begin{aligned} \frac{\partial U(0, y_2)}{\partial n_1} &= g_1(0, y_2) \text{ or } U(0, y_2) = s_1(0, y_2); \\ \frac{\partial U(y_1, 0)}{\partial n_2} &= g_2(y_1, 0) \text{ or } U(y_1, 0) = s_2(y_1, 0); \\ \frac{\partial U(y_1, a_2)}{\partial n_2} &= g_3(y_1, a_2) \text{ or } U(y_1, a_2) = s_3(y_1, a_2). \end{aligned} \quad (5.2)$$

The solutions of these boundary value Problem (P2C)s are expressed via respective Green functions in the form of following integral formula:

$$\begin{aligned} U(x_1, x_2) &= \int_0^{\infty} \int_0^{a_2} f(\xi_1, \xi_2) G(x_1, \xi_1; x_2, \xi_2) d\xi_1 d\xi_2 + \\ &\int_0^{a_2} \left[\frac{\partial U(0, y_2)}{\partial n_1} G(0, x_1; y_2, x_2) - U(0, y_2) \frac{\partial G(0, x_1; y_2, x_2)}{\partial n_1} \right] dy_2 + \\ &\int_0^{\infty} \left[\frac{\partial U(y_1, 0)}{\partial n_2} G(y_1, x_1; 0, x_2) - U(y_1, 0) \frac{\partial G(y_1, x_1; 0, x_2)}{\partial n_2} \right] dy_1 + \\ &\int_0^{\infty} \left[\frac{\partial U(y_1, a_2)}{\partial n_2} G(y_1, x_1; a_2, x_2) - U(y_1, a_2) \frac{\partial G(y_1, x_1; a_2, x_2)}{\partial n_2} \right] dy_1. \end{aligned} \quad (5.3)$$

In eq. (5.3) Green functions G and functions U satisfy Poisson equations

$$\begin{aligned} \nabla^2 G(x_1, \xi_1; x_2, \xi_2) &= -\delta(x - \xi); \\ \nabla^2 U(x_1, x_2) &= -f(x_1, x_2) \end{aligned} \quad (5.4)$$

and the boundary conditions in the following Problems:

Problems (P2C) 5.1- (P2C) 5.8

To construct the Green's functions $G^{(j)}$, ($j=1-8$) for Poisson's equation

$\nabla^2 G(x, \xi) = -\delta(x - \xi)$ for the half-strip ($0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2$) under the following homogeneous boundary conditions

Problem (P2C) 5.1

$$G^{(1)} = 0, \begin{cases} x_1 = 0; & 0 \leq x_2 \leq a_2; & U(0, y_2) = s_1(0, y_2); \\ x_2 = 0, a_2; & 0 \leq x_1 \leq \infty; & U(y_1, 0) = s_2(y_1, 0); \\ x_2 = a_2; & 0 \leq x_1 \leq \infty; & U(y_1, a_2) = s_3(y_1, a_2). \end{cases}$$

The Answer to Problem (P2C) 5.1 for half-strip (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 5.2

$$\begin{aligned} \frac{\partial G^{(2)}}{\partial x_1} &= 0; & x_1 = 0, & 0 \leq x_2 \leq a_2; & \partial U(0, y_2) / \partial n_1 &= g_1(0, y_2); \\ \frac{\partial G^{(2)}}{\partial x_2} &= 0; & x_2 = 0, & 0 \leq x_1 \leq \infty; & \partial U(y_1, 0) / \partial n_2 &= g_2(y_1, 0); \\ \frac{\partial G^{(2)}}{\partial x_2} &= 0; & x_2 = a_2, & 0 \leq x_1 \leq \infty; & \partial U(y_1, a_2) / \partial n_2 &= g_3(y_1, a_2). \end{aligned}$$

The Answer to Problem (P2C) 5.2 for half-strip (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 5.3

$$\begin{aligned} G^{(3)} &= 0; & x_1 = 0, & 0 \leq x_2 \leq a_2; & U(0, y_2) &= s_1(0, y_2); \\ \frac{\partial G^{(3)}}{\partial x_2} &= 0; & x_2 = 0, & 0 \leq x_1 \leq \infty; & \partial U(y_1, 0) / \partial n_2 &= g_2(y_1, 0); \\ \frac{\partial G^{(3)}}{\partial x_2} &= 0; & x_2 = a_2, & 0 \leq x_1 \leq \infty; & \partial U(y_1, a_2) / \partial n_2 &= g_3(y_1, a_2). \end{aligned}$$

The Answer to Problem (P2C) 5.3 for half-strip (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 5.4

$$\frac{\partial \mathcal{G}^{(4)}}{\partial x_1} = 0; \quad x_1 = 0, \quad 0 \leq x_2 \leq a_2; \quad \partial U(0, y_2) / \partial n_1 = g_1(0, y_2);$$

$$G^{(4)} = 0; \quad x_2 = 0; \quad 0 \leq x_1 \leq \infty; \quad U(y_1, 0) = s_2(y_1, 0);$$

$$G^{(4)} = 0; \quad x_2 = a_2, \quad 0 \leq x_1 \leq \infty; \quad U(y_1, a_2) = s_3(y_1, a_2).$$

The Answer to Problem (P2C) 5.4 for half-strip (Green's function for Poisson's equation) can be found in the following books:

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2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 5.5

$$G^{(5)} = 0; \quad \begin{cases} x_1 = 0, \quad 0 \leq x_2 \leq a_2 & U(0, y_2) = s_1(0, y_2); \\ x_2 = 0, \quad 0 \leq x_1 \leq \infty & U(y_1, 0) = s_2(y_1, 0); \end{cases}$$

$$\frac{\partial \mathcal{G}^{(5)}}{\partial x_2} = 0; \quad x_2 = a_2, \quad 0 \leq x_1 \leq \infty; \quad \partial U(y_1, a_2) / \partial n_2 = g_3(y_1, a_2).$$

The Answer to Problem (P2C) 5.5 for half-strip (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 5.6

$$\frac{\partial \mathcal{G}^{(6)}}{\partial x_1} = 0; \quad x_1 = 0, \quad 0 \leq x_2 \leq a_2; \quad \partial U(0, y_2) / \partial n_1 = g_1(0, y_2);$$

$$\frac{\partial \mathcal{G}^{(6)}}{\partial x_2} = 0; \quad x_2 = 0, \quad 0 \leq x_1 \leq \infty; \quad \partial U(y_1, 0) / \partial n_2 = g_2(y_1, 0);$$

$$G^{(6)} = 0; \quad x_2 = a_2, \quad 0 \leq x_1 \leq \infty; \quad U(y_1, a_2) = s_3(y_1, a_2)$$

The Answer to Problem (P2C) 5.6 for half-strip (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermomagneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 5.7

$$G^{(7)} = 0 \begin{cases} x_1 = 0, & 0 \leq x_2 \leq a_2 & U(0, y_2) = s_1(0, y_2); \\ x_2 = a_2, & 0 \leq x_1 \leq \infty; & U(y_1, a_2) = s_3(y_1, a_2). \end{cases}$$

$$\frac{\partial \mathcal{G}^{(7)}}{\partial x_2} = 0; \quad x_2 = 0, \quad 0 \leq x_1 \leq \infty; \quad \partial U(y_1, 0) / \partial n_2 = g_2(y_1, 0).$$

The Answer to Problem (P2C) 5.7 for half-strip (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermomagneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 5.8

$$\frac{\partial G^{(8)}}{\partial x_1} = 0; \quad x_1 = 0, \quad 0 \leq x_2 \leq a_2; \quad \partial U(0, y_2)/\partial n_1 = g_1(0, y_2);$$

$$G^{(8)} = 0; \quad x_2 = 0; \quad 0 \leq x_1 \leq \infty; \quad U(y_1, 0) = s_2(y_1, 0);$$

$$\frac{\partial G^{(8)}}{\partial x_2} = 0; \quad x_2 = a_2; \quad 0 \leq x_1 \leq \infty; \quad \partial U(y_1, a_2)/\partial n_2 = g_3(y_1, a_2)$$

The Answer to Problem (P2C) 5.8 for half-strip (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

(P2C) 6. Rectangle ($0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2$)

In this section formulates 16 boundary-value Problem (P2C)s on constructing Green's functions, $G^{(j)}$, ($j=1-16$), of Poisson's equation for t

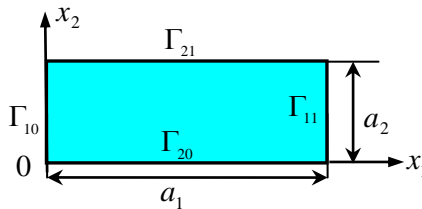


Figure 6: Rectangle with boundary segments of straight lines Γ_{10}, Γ_{11} and Γ_{20}, Γ_{21} .

(P2C) 6.1. Boundary-value Problems and integral representation via Green's functions

Let us consider the following boundary value Problem (P2C)s which consist from the Poisson equation

$$\nabla^2 U(x_1, x_2) = -f(x_1, x_2) \tag{6.1}$$

in the inner points of the quadrant. On the boundaries are given four of the following eight functions:

$$\begin{aligned}
 \frac{\partial U(0, y_2)}{\partial n_1} &= g_1(0, y_2) \text{ or } U(0, y_2) = s_1(0, y_2); \\
 \frac{\partial U(a_1, y_2)}{\partial n_1} &= g_4(a_1, y_2) \text{ or } U(a_1, y_2) = s_4(a_1, y_2); \\
 \frac{\partial U(y_1, 0)}{\partial n_2} &= g_2(y_1, 0) \text{ or } U(y_1, 0) = s_2(y_1, 0); \\
 \frac{\partial U(y_1, a_2)}{\partial n_2} &= g_3(y_1, a_2) \text{ or } U(y_1, a_2) = s_3(y_1, a_2).
 \end{aligned} \tag{6.2}$$

The solutions of these boundary value Problem (P2C)s are expressed via respective Green functions in the form of following integral formula:

$$\begin{aligned}
 U(x_1, x_2) &= \int_0^{a_1} \int_0^{a_2} f(\xi_1, \xi_2) G(x_1, \xi_1; x_2, \xi_2) d\xi_1 d\xi_2 + \\
 &\int_0^{a_2} \left[\frac{\partial U(0, y_2)}{\partial n_1} G(0, x_1; y_2, x_2) - U(0, y_2) \frac{\partial G(0, x_1; y_2, x_2)}{\partial n_1} \right] dy_2 + \\
 &\int_0^{a_2} \left[\frac{\partial U(a_1, y_2)}{\partial n_1} G(a_1, x_1; y_2, x_2) - U(a_1, y_2) \frac{\partial G(a_1, x_1; y_2, x_2)}{\partial n_1} \right] dy_2 + \\
 &\int_0^{a_1} \left[\frac{\partial U(y_1, 0)}{\partial n_2} G(y_1, x_1; 0, x_2) - U(y_1, 0) \frac{\partial G(y_1, x_1; 0, x_2)}{\partial n_2} \right] dy_1 + \\
 &\int_0^{a_1} \left[\frac{\partial U(y_1, a_2)}{\partial n_2} G(y_1, x_1; a_2, x_2) - U(y_1, a_2) \frac{\partial G(y_1, x_1; a_2, x_2)}{\partial n_2} \right] dy_1.
 \end{aligned} \tag{6.3}$$

In eq. (6.3) Green functions G and functions U satisfy Poisson equations

$$\begin{aligned}
 \nabla^2 G(x_1, \xi_1; x_2, \xi_2) &= -\delta(x - \xi); \\
 \nabla^2 U(x_1, x_2) &= -f(x_1, x_2)
 \end{aligned} \tag{6.4}$$

and the following boundary conditions:

Problems (P2C)6.1- (P2C)6.16

To construct the Green's functions $G^{(j)}$, ($j = 1 - 16$) for Poisson's equation $\nabla^2 G(x, \xi) = -\delta(x - \xi)$ for the rectangle ($0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2$) under the following homogeneous boundary conditions

Problem (P2C) 6.1

$$\begin{aligned}
G^{(1)} &= 0; x_1 = 0; 0 \leq x_2 \leq a_2; U(0, y_2) = s_1(0, y_2); \\
G^{(1)} &= 0; x_1 = a_1; 0 \leq x_2 \leq a_2; U(a_1, y_2) = s_4(a_1, y_2); \\
G^{(1)} &= 0; x_2 = 0; 0 \leq x_1 \leq a_1; U(y_1, 0) = s_2(y_1, 0); \\
G^{(1)} &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1; U(y_1, a_2) = s_3(y_1, a_2).
\end{aligned}$$

The Answer to Problem (P2C) 6.1 for rectangle (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 6.2

$$\begin{aligned}
\frac{\partial G^{(2)}}{\partial x_1} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2; \frac{\partial U(0, y_2)}{\partial n_1} = g_1(0, y_2); \\
\frac{\partial G^{(2)}}{\partial x_1} &= 0; x_1 = a_1; 0 \leq x_2 \leq a_2; \frac{\partial U(a_1, y_2)}{\partial n_1} = g_4(a_1, y_2); \\
\frac{\partial G^{(2)}}{\partial x_2} &= 0; x_2 = 0; 0 \leq x_1 \leq a_1; \frac{\partial U(y_1, 0)}{\partial n_2} = g_2(y_1, 0); \\
\frac{\partial G^{(2)}}{\partial x_2} &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1; \frac{\partial U(y_1, a_2)}{\partial n_2} = g_3(y_1, a_2).
\end{aligned}$$

The Answer to Problem (P2C) 6.2 for rectangle (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 6.3

$$\begin{aligned}
G^{(3)} &= 0; x_1 = 0; 0 \leq x_2 \leq a_2; U(0, y_2) = s_1(0, y_2); \\
G^{(3)} &= 0; x_1 = a_1; 0 \leq x_2 \leq a_2; U(a_1, y_2) = s_4(a_1, y_2); \\
\frac{\partial G^{(3)}}{\partial x_2} &= 0; x_2 = 0; 0 \leq x_1 \leq a_1; \frac{\partial U(y_1, 0)}{\partial n_2} = g_2(y_1, 0); \\
\frac{\partial G^{(3)}}{\partial x_2} &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1; \frac{\partial U(y_1, a_2)}{\partial n_2} = g_3(y_1, a_2).
\end{aligned}$$

The Answer to Problem (P2C) 6.3 for rectangle (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 6.4

$$\begin{aligned}
\frac{\partial G^{(4)}}{\partial x_1} &= 0; x_1 = 0; 0 \leq x_2 \leq a_2; \frac{\partial U(0, y_2)}{\partial n_1} = g_1(0, y_2); \\
\frac{\partial G^{(4)}}{\partial x_1} &= 0; x_1 = a_1; 0 \leq x_2 \leq a_2; \frac{\partial U(a_1, y_2)}{\partial n_1} = g_4(a_1, y_2); \\
G^{(4)} &= 0; x_2 = 0; 0 \leq x_1 \leq a_1; U(y_1, 0) = s_2(y_1, 0); \\
G^{(4)} &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1; U(y_1, a_2) = s_3(y_1, a_2).
\end{aligned}$$

The Answer to Problem (P2C) 6.4 for rectangle (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 6.5

$$\begin{aligned}
& G^{(5)} = 0; x_1 = 0; 0 \leq x_2 \leq a_2; U(0, y_2) = s_1(0, y_2); \\
& \frac{\partial G^{(5)}}{\partial x_1} = 0; x_1 = a_1; 0 \leq x_2 \leq a_2; \frac{\partial U(a_1, y_2)}{\partial n_1} = g_4(a_1, y_2); \\
& G^{(5)} = 0; x_2 = 0; 0 \leq x_1 \leq a_1; U(y_1, 0) = s_2(y_1, 0); \\
& G^{(5)} = 0; x_2 = a_2; 0 \leq x_1 \leq a_1; U(y_1, a_2) = s_3(y_1, a_2).
\end{aligned}$$

The Answer to Problem (P2C) 6.5 for rectangle (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 6.6

$$\begin{aligned}
& \frac{\partial G^{(6)}}{\partial x_1} = 0; x_1 = 0; 0 \leq x_2 \leq a_2; \frac{\partial U(0, y_2)}{\partial n_1} = g_1(0, y_2); \\
& G^{(6)} = 0; x_1 = a_1; 0 \leq x_2 \leq a_2; U(a_1, y_2) = s_4(a_1, y_2); \\
& \frac{\partial G^{(6)}}{\partial x_2} = 0; x_2 = 0; 0 \leq x_1 \leq a_1; \frac{\partial U(y_1, 0)}{\partial n_2} = g_2(y_1, 0); \\
& \frac{\partial G^{(6)}}{\partial x_2} = 0; x_2 = a_2; 0 \leq x_1 \leq a_1; \frac{\partial U(y_1, a_2)}{\partial n_2} = g_3(y_1, a_2).
\end{aligned}$$

The Answer to Problem (P2C) 6.6 for rectangle (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 6.7

$$\begin{aligned}
G^{(7)} &= 0; x_1 = 0; 0 \leq x_2 \leq a_2; U(0, y_2) = s_1(0, y_2); \\
\frac{\partial G^{(7)}}{\partial x_1} &= 0; x_1 = a_1; 0 \leq x_2 \leq a_2; \frac{\partial U(a_1, y_2)}{\partial n_1} = g_4(a_1, y_2); \\
\frac{\partial G^{(7)}}{\partial x_2} &= 0; x_2 = 0; 0 \leq x_1 \leq a_1; \frac{\partial U(y_1, 0)}{\partial n_2} = g_2(y_1, 0); \\
\frac{\partial G^{(7)}}{\partial x_2} &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1; \frac{\partial U(y_1, a_2)}{\partial n_2} = g_3(y_1, a_2).
\end{aligned}$$

The Answer to Problem (P2C) 6.7 for rectangle (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 6.8

$$\begin{aligned}
\frac{\partial G^{(8)}}{\partial x_1} &= 0; x_1 = 0; 0 \leq x_2 \leq a_2; \frac{\partial U(0, y_2)}{\partial n_1} = g_1(0, y_2); \\
G^{(8)} &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2; U(a_1, y_2) = s_4(a_1, y_2); \\
G^{(8)} &= 0; x_2 = 0; 0 \leq x_1 \leq a_1; U(y_1, 0) = s_2(y_1, 0); \\
G^{(8)} &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1; U(y_1, a_2) = s_3(y_1, a_2).
\end{aligned}$$

The Answer to Problem (P2C) 6.8 for rectangle (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 6.9

$$\begin{aligned}
& G^{(9)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2; U(0, y_2) = s_1(0, y_2); \\
& G^{(9)} = 0; x_1 = a_1, 0 \leq x_2 \leq a_2; U(a_1, y_2) = s_4(a_1, y_2); \\
& \frac{\partial G^{(9)}}{\partial x_2} = 0; x_2 = 0; 0 \leq x_1 \leq a_1; \frac{\partial U(y_1, 0)}{\partial n_2} = g_2(y_1, 0); \\
& G^{(9)} = 0; x_2 = a_2; 0 \leq x_1 \leq a_1; U(y_1, a_2) = s_3(y_1, a_2).
\end{aligned}$$

The Answer to Problem (P2C) 6.9 for rectangle (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 6.10

$$\begin{aligned}
& G^{(10)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2; U(0, y_2) = s_1(0, y_2); \\
& G^{(10)} = 0; x_1 = a_1, 0 \leq x_2 \leq a_2; U(a_1, y_2) = s_4(a_1, y_2); \\
& G^{(10)} = 0; x_2 = 0; 0 \leq x_1 \leq a_1; U(y_1, 0) = s_2(y_1, 0); \\
& \frac{\partial G^{(10)}}{\partial x_2} = 0; x_2 = a_2; 0 \leq x_1 \leq a_1; \frac{\partial U(y_1, a_2)}{\partial n_2} = g_3(y_1, a_2).
\end{aligned}$$

The Answer to Problem (P2C) 6.10 for rectangle (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 6.11

$$\begin{aligned} \frac{\partial \mathcal{G}^{(11)}}{\partial x_1} &= 0; x_1 = 0; 0 \leq x_2 \leq a_2; \frac{\partial U(0, y_2)}{\partial n_1} = g_1(0, y_2); \\ \frac{\partial \mathcal{G}^{(11)}}{\partial x_1} &= 0; x_1 = a_1; 0 \leq x_2 \leq a_2; \frac{\partial U(a_1, y_2)}{\partial n_1} = g_4(a_1, y_2); \\ G^{(11)} &= 0; x_2 = 0; 0 \leq x_1 \leq a_1; U(y_1, 0) = s_2(y_1, 0); \\ \frac{\partial \mathcal{G}^{(11)}}{\partial x_2} &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1; \frac{\partial U(y_1, a_2)}{\partial n_2} = g_3(y_1, a_2). \end{aligned}$$

The Answer to Problem (P2C) 6.11 for rectangle (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 6.12

$$\begin{aligned} G^{(12)} &= 0; x_1 = 0; 0 \leq x_2 \leq a_2; U(0, y_2) = s_1(0, y_2); \\ \frac{\partial \mathcal{G}^{(12)}}{\partial x_1} &= 0; x_1 = a_1; 0 \leq x_2 \leq a_2; \frac{\partial U(a_1, y_2)}{\partial n_1} = g_4(a_1, y_2); \\ G^{(12)} &= 0; x_2 = 0; 0 \leq x_1 \leq a_1; U(y_1, 0) = s_2(y_1, 0); \\ \frac{\partial \mathcal{G}^{(12)}}{\partial x_2} &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1; \frac{\partial U(y_1, a_2)}{\partial n_2} = g_3(y_1, a_2). \end{aligned}$$

The Answer to Problem (P2C) 6.12 for rectangle (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 6.13

$$\frac{\mathcal{A}G^{(13)}}{\hat{\alpha}_1} = 0; x_1 = 0; 0 \leq x_2 \leq a_2; \frac{\partial U(0, y_2)}{\partial n_1} = g_1(0, y_2);$$

$$G^{(13)} = 0; x_1 = a_1; 0 \leq x_2 \leq a_2; U(a_1, y_2) = s_4(a_1, y_2);$$

$$G^{(13)} = 0; x_2 = 0; 0 \leq x_1 \leq a_1; U(y_1, 0) = s_2(y_1, 0);$$

$$\frac{\mathcal{A}G^{(13)}}{\hat{\alpha}_2} = 0; x_2 = a_2; 0 \leq x_1 \leq a_1; \frac{\partial U(y_1, a_2)}{\partial n_2} = g_3(y_1, a_2).$$

The Answer to Problem (P2C) 6.13 for rectangle (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 6.14

$$\frac{\mathcal{A}G^{(14)}}{\hat{\alpha}_1} = 0; x_1 = 0, a_1; 0 \leq x_2 \leq a_2; \frac{\partial U(0, y_2)}{\partial n_1} = g_1(0, y_2);$$

$$\frac{\mathcal{A}G^{(14)}}{\hat{\alpha}_1} = 0; x_1 = 0, a_1; 0 \leq x_2 \leq a_2; \frac{\partial U(a_1, y_2)}{\partial n_1} = g_4(a_1, y_2);$$

$$\frac{\mathcal{A}G^{(14)}}{\hat{\alpha}_2} = 0; x_2 = 0; 0 \leq x_1 \leq a_1; \frac{\partial U(y_1, 0)}{\partial n_2} = g_2(y_1, 0);$$

$$G^{(14)} = 0; x_2 = a_2; 0 \leq x_1 \leq a_1; U(y_1, a_2) = s_3(y_1, a_2).$$

The Answer to Problem (P2C) 6.14 for rectangle (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 6.15

$$\begin{aligned}
& G^{(15)} = 0; x_1 = 0; 0 \leq x_2 \leq a_2; U(0, y_2) = s_1(0, y_2); \\
& \frac{\partial G^{(15)}}{\partial x_1} = 0; x_1 = a_1; 0 \leq x_2 \leq a_2; \frac{\partial U(a_1, y_2)}{\partial n_1} = g_4(a_1, y_2); \\
& \frac{\partial G^{(15)}}{\partial x_2} = 0; x_2 = 0; 0 \leq x_1 \leq a_1; \frac{\partial U(y_1, 0)}{\partial n_2} = g_2(y_1, 0); \\
& G^{(15)} = 0; x_2 = a_2; 0 \leq x_1 \leq a_1; U(y_1, a_2) = s_3(y_1, a_2)
\end{aligned}$$

The Answer to Problem (P2C) 6.15 for rectangle (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P2C) 6.16

$$\begin{aligned}
& \frac{\partial G^{(16)}}{\partial x_1} = 0; x_1 = 0; 0 \leq x_2 \leq a_2; \frac{\partial U(0, y_2)}{\partial n_1} = g_1(0, y_2); \\
& G^{(16)} = 0; x_1 = a_1; 0 \leq x_2 \leq a_2; U(a_1, y_2) = s_4(a_1, y_2); \\
& \frac{\partial G^{(16)}}{\partial x_2} = 0; x_2 = 0; 0 \leq x_1 \leq a_1; \frac{\partial U(y_1, 0)}{\partial n_2} = g_2(y_1, 0); \\
& G^{(16)} = 0; x_2 = a_2; 0 \leq x_1 \leq a_1; U(y_1, a_2) = s_3(y_1, a_2)
\end{aligned}$$

The Answer to Problem (P2C) 6.16 for rectangle (Green's function for Poisson's equation) can be found in the following books:

1. Victor Seremet & Guy Bonnet, Encyclopedia of Domain Green's Functions (Thermo-magneto-electrostatics of solids in rectangular and polar coordinates), State Agrarian University of Moldova: Publisher Center of UASM, Chisinau, Moldova, 2008, 220 pag., (in English).
2. Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)