

List of Boundary-value Problem (P3C) s for 3D Cartesian Domains, for which the Green's Functions for Poisson's Equation have been derived

Green's functions to these Problems can be found in the book:

Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

(P3C) 1. Space $(-\infty \leq x_1, x_2, x_3 \leq \infty)$

This Section formulates a boundary-value Problem (P3C) on constructing Green's function, G of Poisson equation for the space, final Answer to it provided.

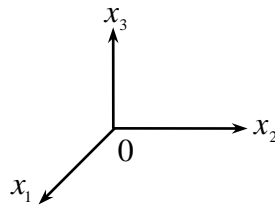


Figure 13: Space in Cartesian co-ordinates.

(P3C) 1.1. Boundary-value Problem (P3C)

Let us consider the following boundary value Problem (P3C) s which consist from the Poisson equation

$$\begin{aligned}\nabla^2 G(x_1, \xi_1; x_2, \xi_2) &= -\delta(x - \xi); \\ \nabla^2 U(x_1, x_2) &= -f(x_1, x_2).\end{aligned}$$

in the inner points of the space. At infinity the functions G and U must vanish.

Problem (P3C).1 To construct the Green's function $G(x, \xi)$ for Poisson's equation $\nabla^2 G(x, \xi) = -\delta(x - \xi)$ for the space $(-\infty \leq x_1, x_2, x_3 \leq \infty)$.

The Answer to Problem (P3C).1 for space (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

(P3C)2. Half-space $(0 \leq x_1 \leq \infty, -\infty \leq x_2, x_3 \leq \infty)$

This section formulates two boundary-value Problem (P3C) s on constructing Green's functions, $G^{(j)}$, ($j = 1-2$), of Poisson's equation for the half-space

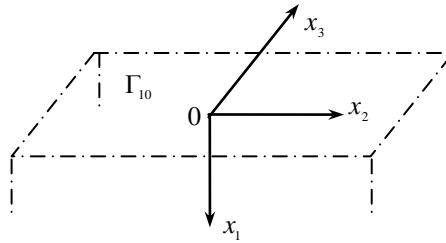


Figure 2: Half-space with boundary plane Γ_{10} .

(P3C) 2.1. Boundary-value Problems

Let us consider the following boundary value Problem (P3C) s which consist from the Poisson equation

$$\nabla^2 U(x_1, x_2) = -f(x_1, x_2)$$

in the inner points of the half-space. At infinity the functions U must vanish. On the boundaries, one of the following two functions are given:

$$\partial U(0, y_2, y_3) / \partial n_1 = g_1(0, y_2, y_3) \text{ or } U(0, y_2, y_3) = s_1(0, y_2, y_3)$$

$$\nabla^2 G(x_1, \xi_1; x_2, \xi_2) = -\delta(x - \xi)$$

and the boundary conditions defined below for each Problem (P3C) .

Problems (P3C) 2.1- (P3C)2.2

To construct the Green's functions for Poisson's equation $\nabla^2 G(x, \xi) = -\delta(x - \xi)$ for the half-space ($0 \leq x_1 \leq \infty, -\infty \leq x_2, x_3 \leq \infty$) under the following boundary conditions:

The solutions of the 16 Problem (P3C) s and their related Green's functions $G^{(j)}$, ($j=1-16$) for Poisson's equation $\nabla^2 G(x, \xi) = -\delta(x - \xi)$ for the rectangular ($0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2$) are given below for the suitable boundary conditions defined in the boxes:

Problem (P3C) 2.1

$$G^{(1)} = 0; \quad x_1 = 0, \quad -\infty \leq x_2, x_3 \leq \infty; \quad U(0, y_2, y_3) = S(0, y_2, y_3)$$

The Answer to Problem (P3C) 2.1 for half-space (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 2.2

$$\partial G^{(2)} / \partial x_1 = 0; \quad x_1 = 0, \quad -\infty \leq x_2, x_3 \leq \infty. \quad \partial U / \partial n_1 = g(0, y_2, y_3)$$

Problem (P3C) 2.2 for half-space (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

(P3C)3. Quarter-space ($0 \leq x_1, x_2 \leq \infty, -\infty \leq x_3 \leq \infty$)

This Section formulates four boundary-value Problem (P3C) s on constructing Green's functions, $G^{(j)}$, ($j=1-4$), of Poisson's equation for the quarter-space

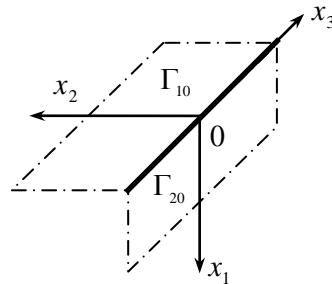


Figure 3: Quarter-space with boundary half-planes Γ_{10} and Γ_{20} .

Let us consider the following boundary value Problem (P3C) s which consist from the Poisson equation

$$\begin{aligned} \nabla^2 G(x_1, \xi_1; x_2, \xi_2) &= -\delta(x - \xi); \\ \nabla^2 U(x_1, x_2) &= -f(x_1, x_2). \end{aligned}$$

in the inner points of the half-space. At infinity the functions G and U must vanish.

To construct the Green's functions $G^{(j)}$, ($j=1-4$) for Poisson's equation $\nabla^2 G(x, \xi) = -\delta(x - \xi)$ for the quarter-space ($0 \leq x_1, x_2 \leq \infty, -\infty \leq x_3 \leq \infty$) under the following homogeneous boundary conditions:

Problem (P3C) 3.1

$\begin{aligned} G^{(1)} &= 0; x_1 = 0, 0 \leq x_2 \leq \infty, -\infty \leq x_3 \leq \infty; & U(0, y_2, y_3) &= s_1(0, y_2, y_3); \\ G^{(2)} &= 0; x_2 = 0, 0 \leq x_1 \leq \infty, -\infty \leq x_3 \leq \infty; & U(y_1, 0, y_3) &= s_2(y_1, 0, y_3). \end{aligned}$
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The Answer to Problem (P3C) 3.1 for quarter-space (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 3.2

$$\begin{aligned} \partial G^{(2)}/\partial x_1 = 0; x_1 = 0, 0 \leq x_2 \leq \infty, -\infty \leq x_3 \leq \infty; \partial U(0, y_2, y_3)/\partial n_1 = g_1(0, y_2, y_3); \\ \partial G^{(2)}/\partial x_2 = 0; x_2 = 0, 0 \leq x_1 \leq \infty, -\infty \leq x_3 \leq \infty; \partial U(y_1, 0, y_3)/\partial n_2 = g_2(y_1, 0, y_3) \end{aligned}$$

The Answer to Problem (P3C) 3.2 for quarter-space (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 3.3

$$\begin{aligned} \partial G^{(3)}/\partial x_1 = 0; x_1 = 0, 0 \leq x_2 \leq \infty, -\infty \leq x_3 \leq \infty; \partial U(0, y_2, y_3)/\partial n_1 = g_1(0, y_2, y_3) \\ G^{(3)} = 0; x_2 = 0, 0 \leq x_1 \leq \infty, -\infty \leq x_3 \leq \infty; U(y_1, 0, y_3) = s_2(y_1, 0, y_3) \end{aligned}$$

The Answer to Problem (P3C) 3.3 for quarter-space (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 3.4

$$\begin{aligned} G^{(4)} = 0; x_1 = 0, 0 \leq x_2 \leq \infty, -\infty \leq x_3 \leq \infty; U(0, y_2, y_3) = s_1(0, y_2, y_3); \\ \partial G^{(4)}/\partial x_2 = 0; x_2 = 0, 0 \leq x_1 \leq \infty, -\infty \leq x_3 \leq \infty; \partial U(y_1, 0, y_3)/\partial n_2 = g_2(y_1, 0, y_3) \end{aligned}$$

The Answer to Problem (P3C) 3.4 for quarter-space (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

(P3C)4. Octant ($0 \leq x_1, x_2, x_3 \leq \infty$)

This Section formulates eight boundary-value Problem (P3C) s on constructing Green's functions, $G^{(j)}$, $j = 1-8$, of Poisson's equation for the octant

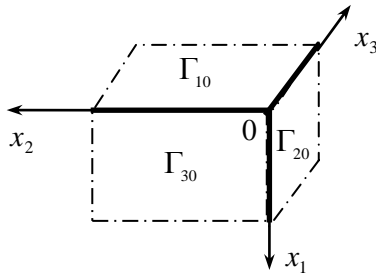


Figure 4: Octant with boundary quadrants Γ_{10} , Γ_{20} and Γ_{30} .

Problems (P3C) 4.1–(P3C)4.8

Let us consider the following boundary value Problem (P3C) s which consist from the Poisson equation

$$\begin{aligned}\nabla^2 G(x_1, \xi_1; x_2, \xi_2) &= -\delta(x - \xi); \\ \nabla^2 U(x_1, x_2) &= -f(x_1, x_2).\end{aligned}$$

in the inner points of the octant. At infinity the functions G and U must vanish.

To construct the Green's functions $G^{(j)}$, $j=1-8$, for Poisson's equation $\nabla^2 G(x, \xi) = -\delta(x - \xi)$ for the octant ($0 \leq x_1, x_2, x_3 \leq \infty$) under the following homogeneous boundary conditions:

Problem (P3C) 4.1

$$\begin{aligned}G^{(1)} &= 0; x_1 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_3 \leq \infty; & U(0, y_2, y_3) &= s_1(0, y_2, y_3); \\ G^{(1)} &= 0; x_2 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq \infty; & U(y_1, 0, y_3) &= s_2(y_1, 0, y_3); \\ G^{(1)} &= 0; x_3 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; & U(y_1, y_2, 0) &= s_3(y_1, y_2, 0).\end{aligned}$$

The Answer to Problem (P3C) 4.1 for octant (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 4.2

$$\begin{aligned}\partial G^{(2)} / \partial x_1 &= 0; x_1 = 0, 0 \leq x_2 \leq \infty; 0 \leq x_3 \leq \infty; & \partial U(0, y_2, y_3) / \partial n_1 &= s_1(0, y_2, y_3); \\ \partial G^{(2)} / \partial x_2 &= 0; x_2 = 0, 0 \leq x_1 \leq \infty; 0 \leq x_3 \leq \infty; & \partial U(y_1, 0, y_3) / \partial n_2 &= s_2(y_1, 0, y_3); \\ \partial G^{(2)} / \partial x_3 &= 0; x_3 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_1 \leq \infty. & \partial U(y_1, y_2, 0) / \partial n_3 &= s_3(y_1, y_2, 0).\end{aligned}$$

The Answer to Problem (P3C) 4.2 for octant (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 4.3

$$G^{(3)} = 0; x_1 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_3 \leq \infty; U(0, y_2, y_3) = s_1(0, y_2, y_3);$$

$$G^{(3)} = 0; x_2 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq \infty; U(y_1, 0, y_3) = s_2(y_1, 0, y_3)$$

$$\partial G^{(3)} / \partial x_3 = 0; x_3 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_1 \leq \infty; \partial U(y_1, y_2, 0) / \partial n_3 = s_3(y_1, y_2, 0).$$

The Answer to Problem (P3C) 4.3 for octant (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 4.4

$$G^{(4)} = 0; x_1 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_3 \leq \infty; U(0, y_2, y_3) = s_1(0, y_2, y_3);$$

$$\partial G^{(4)} / \partial x_2 = 0; x_2 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq \infty; \partial U(y_1, 0, y_3) / \partial n_2 = s_2(y_1, 0, y_3);$$

$$\partial G^{(4)} / \partial x_3 = 0; x_3 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_1 \leq \infty; \partial U(y_1, y_2, 0) / \partial n_3 = s_3(y_1, y_2, 0).$$

The Answer to Problem (P3C) 4.4 for octant (Green's function for Poisson's equation in Cartesian coordinates)

Problem (P3C) 4.5

$$\partial G^{(5)} / \partial x_1 = 0; x_1 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_3 \leq \infty; \partial U(0, y_2, y_3) / \partial n_1 = s_1(0, y_2, y_3);$$

$$G^{(5)} = 0, x_2 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq \infty; U(y_1, 0, y_3) = s_2(y_1, 0, y_3);$$

$$G^{(5)} = 0; x_3 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_1 \leq \infty; U(y_1, y_2, y_3) = s_3(y_1, y_2, y_3).$$

The Answer to Problem (P3C) 4.5 for octant (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 4.6

$$\partial G^{(6)} / \partial x_1 = 0; x_1 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_3 \leq \infty; \partial U(0, y_2, y_3) / \partial n_1 = s_1(0, y_2, y_3);$$

$$\partial G^{(6)} / \partial x_2 = 0, x_2 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq \infty; \partial U(y_1, 0, y_3) / \partial n_2 = s_2(y_1, 0, y_3);$$

$$G^{(6)} = 0; x_3 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_1 \leq \infty. U(y_1, y_2, y_3) = s_3(y_1, y_2, y_3).$$

The Answer to Problem (P3C) 4.6 for octant (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 4.7

$$\begin{aligned} \partial G^{(7)}/\partial x_1 = 0; x_1 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_3 \leq \infty; \partial U(0, y_2, y_3)/\partial n_1 = s_1(0, y_2, y_3); \\ G^{(7)} = 0, x_2 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq \infty; U(y_1, 0, y_3) = s_2(y_1, 0, y_3); \\ \partial G^{(7)}/\partial x_3 = 0; x_3 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_1 \leq \infty; \partial U(y_1, y_2, 0)/\partial n_3 = s_3(y_1, y_2, 0). \end{aligned}$$

The Answer to Problem (P3C) 4.7 for octant (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 4.8

$$\begin{aligned} G^{(8)} = 0; x_1 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_3 \leq \infty; U(0, y_2, y_3) = s_1(0, y_2, y_3); \\ \partial G^{(8)}/\partial x_2 = 0; x_2 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq \infty; \partial U(y_1, 0, y_3)/\partial n_2 = s_2(y_1, 0, y_3); \\ G^{(8)} = 0; x_3 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_1 \leq \infty; U(y_1, y_2, 0) = s_3(y_1, y_2, 0). \end{aligned}$$

The Answer to Problem (P3C) 4.8 for octant (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

(P3C)5. Layer ($-\infty \leq x_1, x_2 \leq \infty, 0 \leq x_3 \leq a_3$)

This section formulates four boundary-value Problem (P3C) s on constructing Green's functions, $G^{(j)}$, ($j=1-4$), of Poisson's equation for the layer

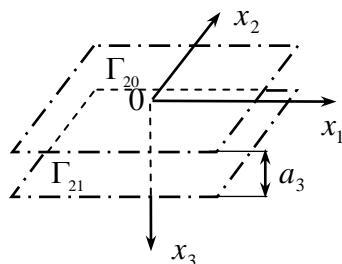


Figure 5: Layer with boundary planes Γ_{20} and Γ_{21} .

Problems (P3C) 5.1– (P3C) 5.4

Let us consider the following boundary value Problem (P3C) s which consist from the Poisson equation

$$\begin{aligned} \nabla^2 G(x_1, \xi_1; x_2, \xi_2) = -\delta(x - \xi); \\ \nabla^2 U(x_1, x_2) = -f(x_1, x_2). \end{aligned}$$

in the inner points of the octant. At infinity the functions G and U must vanish.

To construct the Green's functions $G^{(j)}(x, \xi)$, ($j=1-4$) for Poisson's equation $\nabla^2 G^{(j)}(x, \xi) = -\delta(x - \xi)$ for the layer $(-\infty \leq x_1, x_2 \leq \infty, 0 \leq x_3 \leq a_3)$ under the following homogeneous boundary conditions:

Problem (P3C) 5.1

$$\begin{aligned} G^{(1)} = 0; x_3 = 0, -\infty \leq x_1, x_2 \leq \infty; \quad U(y_1, y_2, 0) = s_3(y_1, y_2, 0); \\ G^{(1)} = 0; x_3 = a_3, -\infty \leq x_1, x_2 \leq \infty; \quad U(y_1, y_2, a_3) = s_3'(y_1, y_2, a_3); \end{aligned}$$

The Answer to Problem (P3C) 5.1 for layer (Green's function for Poisson's equation in Cartesian coordinates)

can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 5.2

$$\begin{aligned} \partial G^{(2)} / \partial x_3 = 0; x_3 = 0, -\infty \leq x_1, x_2 \leq \infty; \quad \partial U(y_1, y_2, 0) / \partial n_3 = g_3(y_1, y_2, 0); \\ \partial G^{(2)} / \partial x_3 = 0; x_3 = a_3, -\infty \leq x_1, x_2 \leq \infty; \quad \partial U(y_1, y_2, 0) / \partial n_3 = g_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 5.2 for layer (Green's function for Poisson's equation in Cartesian coordinates)

can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 5.3

$$\begin{aligned} G^{(3)} = 0, x_3 = 0, -\infty \leq x_3 \leq \infty; \quad U(y_1, y_2, 0) = s_3(y_1, y_2, 0); \\ \partial G^{(3)} / \partial x_3 = 0, x_3 = a_3, -\infty \leq x_3 \leq \infty; \quad \partial U(y_1, y_2, 0) / \partial n_3 = g_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 5.3 for layer (Green's function for Poisson's equation in Cartesian coordinates)

can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 5.4

$$\begin{aligned} \partial G^{(4)} / \partial x_3 = 0; x_3 = 0, -\infty \leq x_1, x_2 \leq \infty; \quad \partial U(y_1, y_2, 0) / \partial n_3 = g_3(y_1, y_2, 0); \\ G^{(4)} = 0; x_3 = a_3, -\infty \leq x_1, x_2 \leq \infty; \quad U(y_1, y_2, a_3) = s_3'(y_1, y_2, a_3) \end{aligned}$$

The Answer to Problem (P3C) 5.4 for layer (Green's function for Poisson's equation in Cartesian coordinates)

can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

(P3C)6. Half-layer ($0 \leq x_1 \leq \infty, -\infty \leq x_2 \leq \infty, 0 \leq x_3 \leq a_3$)

This section formulates eight boundary-value Problem (P3C) s on constructing Green's functions, $G^{(j)}, (j=1-8)$, of Poisson's equation for the half-layer

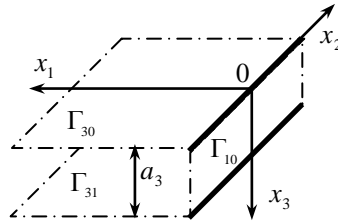


Figure 6: Half-layer with boundary half- planes Γ_{30}, Γ_{31} and boundary strip Γ_{10} .

Problems (P3C) 6.1– (P3C) 6.8

Let us consider the following boundary value Problem (P3C) s which consist from the Poisson equation

$$\begin{aligned}\nabla^2 G(x_1, \xi_1; x_2, \xi_2) &= -\delta(x - \xi); \\ \nabla^2 U(x_1, x_2) &= -f(x_1, x_2).\end{aligned}$$

in the inner points of the half-layer. At infinity the functions G and U must vanish.

To construct the Green's functions $G^{(j)}(x, \xi), (j=1-8)$ for Poisson's equation $\nabla^2 G^{(j)}(x, \xi) = -\delta(x - \xi)$ for the half-layer $(0 \leq x_1 \leq \infty, -\infty \leq x_2 \leq \infty, 0 \leq x_3 \leq a_3)$ under the following homogeneous boundary conditions:

Problem (P3C) 6.1

$$G^{(1)} = 0; \begin{cases} x_1 = 0; & -\infty \leq x_2 \leq \infty, & 0 \leq x_3 \leq a_3; & U = s_1(0, y_2, y_3); \\ x_3 = 0; & 0 \leq x_1 \leq \infty, & -\infty \leq x_2 \leq \infty; & U = s_3(y_1, y_2, 0); \\ x_3 = a_3; & 0 \leq x_1 \leq \infty, & -\infty \leq x_2 \leq \infty; & U = s_3'(y_1, y_2, a_3); \end{cases}$$

The Answer to Problem (P3C) 6.1 for half-layer (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 6.2

$$\begin{aligned}\partial G^{(2)} / \partial x_1 = 0; & x_1 = 0, & -\infty \leq x_2 \leq \infty, & 0 \leq x_3 \leq a_3; & \partial U / \partial y_1 = g_1(0, y_2, y_3); \\ \partial G^{(2)} / \partial x_3 = 0; & x_3 = 0; & 0 \leq x_1 \leq \infty, & -\infty \leq x_2 \leq \infty; & \partial U / \partial y_3 = g_3(y_1, y_2, 0); \\ \partial G^{(2)} / \partial x_3 = 0; & x_3 = a_3; & 0 \leq x_1 \leq \infty, & -\infty \leq x_2 \leq \infty; & \partial U / \partial y_3 = g_3'(y_1, y_2, a_3).\end{aligned}$$

The Answer to Problem (P3C) 6.2 for half-layer (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 6.3

$$\begin{aligned}
G^{(3)} = 0; x_1 = 0, -\infty \leq x_2 \leq \infty, 0 \leq x_3 \leq a_3; \quad U = s_1(0, y_2, y_3) \\
\partial G^{(3)} / \partial x_3 = 0; x_3 = 0; 0 \leq x_1 \leq \infty, -\infty \leq x_2 \leq \infty; \quad \partial U / \partial y_3 = g_3(y_1, y_2, 0); \\
\partial G^{(3)} / \partial x_3 = 0; x_3 = a_3; 0 \leq x_1 \leq \infty, -\infty \leq x_2 \leq \infty; \quad \partial U / \partial y_3 = g_3'(y_1, y_2, a_3)
\end{aligned}$$

The Answer to Problem (P3C) 6.3 for half-layer (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 6.4

$$\begin{aligned}
G^{(4)} = 0; \begin{cases} x_1 = 0, -\infty \leq x_2 \leq \infty, 0 \leq x_3 \leq a_3; & U = s_1(0, y_2, y_3); \\ x_3 = 0, 0 \leq x_1 \leq \infty, -\infty \leq x_2 \leq \infty; & U = s_3(y_1, y_2, 0); \end{cases} \\
\partial G^{(4)} / \partial x_3 = 0; x_3 = a_3; 0 \leq x_1 \leq \infty, -\infty \leq x_2 \leq \infty; \quad \partial U / \partial y_3 = g_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 6.4 for half-layer (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 6.5

$$\begin{aligned}
G^{(5)} = 0; \begin{cases} x_1 = 0, -\infty \leq x_2 \leq \infty, 0 \leq x_3 \leq a_3; & U = s_1(0, y_2, y_3); \\ x_3 = a_3, 0 \leq x_1 \leq \infty, -\infty \leq x_2 \leq \infty; & U = s_3'(y_1, y_2, a_3); \end{cases} \\
\partial G^{(5)} / \partial x_3 = 0; x_3 = 0; 0 \leq x_1 \leq \infty, -\infty \leq x_2 \leq \infty; \quad \partial U / \partial y_3 = g_3'(y_1, y_2, 0).
\end{aligned}$$

The Answer to Problem (P3C) 6.5 for half-layer (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 6.6

$$\begin{aligned}
\partial G^{(6)} / \partial x_1 = 0; x_1 = 0, -\infty \leq x_2 \leq \infty, 0 \leq x_3 \leq a_3; \quad \partial U / \partial y_1 = g_1(0, y_2, y_3); \\
G^{(6)} = 0; x_3 = 0; 0 \leq x_1 \leq \infty, -\infty \leq x_2 \leq \infty; \quad U = s_3(y_1, y_2, 0); \\
G^{(6)} = 0; x_3 = a_3; 0 \leq x_1 \leq \infty, -\infty \leq x_2 \leq \infty; \quad U = s_3'(y_1, y_2, a_3)
\end{aligned}$$

The Answer to Problem (P3C) 6.6 for half-layer (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 6.7

$$\left. \begin{array}{l} \partial G^{(7)}/\partial x_1 = 0; x_1 = 0, -\infty \leq x_2 \leq \infty, 0 \leq x_3 \leq a_3; \partial U/\partial y_1 = g_1(0, y_2, y_3); \\ G^{(7)} = 0; x_3 = 0, \\ \partial G^{(7)}/\partial x_3 = 0; x_3 = a_3 \end{array} \right\}, 0 \leq x_1 \leq \infty, -\infty \leq x_2 \leq \infty, \left\{ \begin{array}{l} U = s_3(y_1, y_2, 0); \\ \partial U/\partial y_3 = g_3'(y_1, y_2, a_3). \end{array} \right.$$

The Answer to Problem (P3C) 6.7 for half-layer (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 6.8

$$\left. \begin{array}{l} \partial G^{(8)}/\partial x_1 = 0; x_1 = 0, -\infty \leq x_2 \leq \infty, 0 \leq x_3 \leq a_3; \partial U/\partial y_1 = g_1(0, y_2, y_3); \\ \partial G^{(8)}/\partial x_3 = 0; x_3 = 0, \\ G^{(8)} = 0; x_3 = a_3 \end{array} \right\}, 0 \leq x_1 \leq \infty, -\infty \leq x_2 \leq \infty; \left\{ \begin{array}{l} \partial U/\partial y_3 = g_3(y_1, y_2, 0); \\ U = s_3'(y_1, y_2, a_3). \end{array} \right.$$

The Answer to Problem (P3C) 6.8 for half-layer (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

(P3C)7. Quarter-layer ($0 \leq x_1, x_2 \leq \infty, 0 \leq x_3 \leq a_3$)

This Section formulates 16 boundary-value Problem (P3C) s on constructing Green's functions, $G^{(j)}$, ($j=1-16$), of Poisson's equation for the quarter-layer

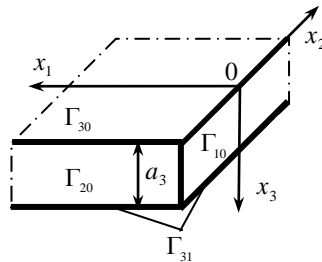


Figure 7: Quarter-layer with boundary quadrants Γ_{30}, Γ_{31} and boundary half-strips Γ_{10}, Γ_{20} .

Problems (P3C)7.1– (P3C) 7.16

To construct the Green's functions $G^{(j)}(x, \xi)$, ($j=1-16$) for Poisson's equation $\nabla^2 G^{(j)}(x, \xi) = -\delta(x - \xi)$ for the quarter-layer ($0 \leq x_1, x_2 \leq \infty, 0 \leq x_3 \leq a_3$) under the following homogeneous boundary conditions:

Problem (P3C) 7.1

$$\begin{aligned}
G^{(1)} &= 0; x_1 = 0; 0 \leq x_2 \leq \infty, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
G^{(1)} &= 0; x_2 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
G^{(1)} &= 0; x_3 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; U = s_3(y_1, y_2, 0); \\
G^{(1)} &= 0; x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 7.1 for quarter-layer (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 7.2

$$\begin{aligned}
\partial G^{(2)} / \partial x_1 &= 0; x_1 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial y_1 = g_1(0, y_2, y_3); \\
\partial G^{(2)} / \partial x_2 &= 0; x_2 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial y_2 = g_2(y_1, 0, y_3); \\
\partial G^{(2)} / \partial x_3 &= 0; x_3 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; \partial U / \partial y_3 = g_3(y_1, y_2, 0); \\
\partial G^{(2)} / \partial x_3 &= 0; x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; \partial U / \partial y_3 = g_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 7.2 for quarter-layer (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 7.3

$$\begin{aligned}
G^{(3)} &= 0; x_1 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
G^{(3)} &= 0; x_2 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
\partial G^{(3)} / \partial x_3 &= 0; x_3 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; \partial U / \partial y_3 = g_3(y_1, y_2, 0); \\
\partial G^{(3)} / \partial x_3 &= 0; x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; \partial U / \partial y_3 = g_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 7.3 for quarter-layer (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 7.4

$$\begin{aligned}
G^{(4)} &= 0; x_1 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
G^{(4)} &= 0; x_2 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
G^{(4)} &= 0; x_3 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_3(y_1, y_2, 0); \\
\partial G^{(4)} / \partial x_3 &= 0; x_3 = a_3, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; \partial U / \partial y_3 = g_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 7.4 for quarter-layer (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 7.5

$$\begin{aligned}
G^{(5)} &= 0; \quad x_1 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
G^{(5)} &= 0; \quad x_2 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
\partial G^{(5)} / \partial x_3 &= 0; \quad x_3 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; \partial U / \partial y_3 = g_3(y_1, y_2, 0); \\
G^{(5)} &= 0; \quad x_3 = a_3, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 7.5 for quarter-layer (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 7.6

$$\begin{aligned}
G^{(6)} &= 0; \quad x_1 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
\partial G^{(6)} / \partial x_2 &= 0; \quad x_2 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial y_2 = g_2(y_1, 0, y_3); \\
\partial G^{(6)} / \partial x_3 &= 0; \quad x_3 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; \partial U / \partial y_3 = g_3(y_1, y_2, 0); \\
\partial G^{(6)} / \partial x_3 &= 0; \quad x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; \partial U / \partial y_3 = g_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 7.6 for quarter-layer (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 7.7

$$\begin{aligned}
G^{(7)} &= 0; \quad x_1 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_3 \leq a_3; s_1(0, y_2, y_3); \\
\partial G^{(7)} / \partial x_2 &= 0; \quad x_2 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial y_2 = g_2(y_1, 0, y_3); \\
G^{(7)} &= 0; \quad x_3 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; U = s_3(y_1, y_2, 0); \\
G^{(7)} &= 0; \quad x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 7.7 for quarter-layer (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 7.8

$$\begin{aligned}
G^{(8)} &= 0; \quad x_1 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_3 \leq a_3; s_1(0, y_2, y_3); \\
\partial G^{(8)} / \partial x_2 &= 0; \quad x_2 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial y_2 = g_2(y_1, 0, y_3); \\
G^{(8)} &= 0; \quad x_3 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; U = s_3(y_1, y_2, 0); \\
\partial G^{(8)} / \partial x_3 &= 0; \quad x_3 = a_3, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; \partial U / \partial y_3 = g_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 7.8 for quarter-layer (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 7.9

$$\begin{aligned}
G^{(9)} &= 0; \quad x_1 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
\partial G^{(9)} / \partial x_2 &= 0; \quad x_2 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial y_2 = g_2(y_1, 0, y_3); \\
\partial G^{(9)} / \partial x_3 &= 0; \quad x_3 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; \partial U / \partial y_3 = g_3(y_1, y_2, 0); \\
G^{(9)} &= 0; \quad x_3 = a_3, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; U = s'_3(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 7.9 for quarter-layer (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 7.10

$$\begin{aligned}
\partial G^{(10)} / \partial x_1 &= 0; \quad x_1 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial y_1 = g_1(0, y_2, y_3); \\
\partial G^{(10)} / \partial x_2 &= 0; \quad x_2 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial y_2 = g_2(y_1, 0, y_3); \\
G^{(10)} &= 0; \quad x_3 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; U = s_3(y_1, y_2, 0); \\
G^{(10)} &= 0; \quad x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; U = s'_3(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 7.10 for quarter-layer (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 7.11

$$\begin{aligned}
\partial G^{(11)} / \partial x_1 &= 0; \quad x_1 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial y_1 = g_1(0, y_2, y_3); \\
\partial G^{(11)} / \partial x_2 &= 0; \quad x_2 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial y_2 = g_2(y_1, 0, y_3); \\
G^{(11)} &= 0; \quad x_3 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; U = s_3(y_1, y_2, 0); \\
\partial G^{(11)} / \partial x_3 &= 0; \quad x_3 = a_3, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; \partial U / \partial y_3 = g'_3(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 7.11 for quarter-layer (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 7.12

$$\begin{aligned}
\partial G^{(12)} / \partial x_1 &= 0; \quad x_1 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial y_1 = g_1(0, y_2, y_3); \\
\partial G^{(12)} / \partial x_2 &= 0; \quad x_2 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial y_2 = g_2(y_1, 0, y_3); \\
\partial G^{(12)} / \partial x_3 &= 0; \quad x_3 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; \partial U / \partial y_3 = g_3(y_1, y_2, 0); \\
G^{(12)} &= 0; \quad x_3 = a_3, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; U = s'_3(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 7.12 for quarter-layer (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 7.13

$$\begin{aligned} \partial G^{(13)} / \partial x_1 &= 0; \quad x_1 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial y_1 = g_1(0, y_2, y_3); \\ G^{(13)} &= 0; \quad x_2 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ G^{(13)} &= 0; \quad x_3 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; U = s_3(y_1, y_2, 0); \\ G^{(13)} &= 0; \quad x_3 = a_3, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; U = s_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 7.13 for quarter-layer (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 7.14

$$\begin{aligned} \partial G^{(14)} / \partial x_1 &= 0; \quad x_1 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial y_1 = g_1(0, y_2, y_3); \\ G^{(14)} &= 0; \quad x_2 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ \partial G^{(14)} / \partial x_3 &= 0; \quad x_3 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; \partial U / \partial y_3 = g_3(y_1, y_2, 0); \\ \partial G^{(14)} / \partial x_3 &= 0; \quad x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; \partial U / \partial y_3 = g_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 7.14 for quarter-layer (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 7.15

$$\begin{aligned} \partial G^{(15)} / \partial x_1 &= 0; \quad x_1 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial y_1 = g_1(0, y_2, y_3); \\ G^{(15)} &= 0; \quad x_2 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ G^{(15)} &= 0; \quad x_3 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; U = s_3(y_1, y_2, 0); \\ \partial G^{(15)} / \partial x_3 &= 0; \quad x_3 = a_3, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; \partial U / \partial y_3 = g_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 7.15 for quarter-layer (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 7.16

$$\begin{aligned} \partial G^{(16)} / \partial x_1 &= 0; \quad x_1 = 0, 0 \leq x_2 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial y_1 = g_1(0, y_2, y_3); \\ G^{(16)} &= 0; \quad x_2 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \quad U = s_2(y_1, 0, y_3); \\ \partial G^{(16)} / \partial x_3 &= 0; \quad x_3 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; \partial U / \partial y_3 = g_3(y_1, y_2, 0); \\ G^{(16)} &= 0; \quad x_3 = a_3, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq \infty; U = s_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 7.16 for quarter-layer (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

(P3C)8. Unbounded Parallelepiped $(-\infty \leq x_1 \leq \infty; 0 \leq x_2 \leq a_2; 0 \leq x_3 \leq a_3)$

In this section formulates 16 boundary-value Problem (P3C) s on constructing Green's functions, $G^{(j)}$, ($j=1-16$), of Poisson's equation for the unbounded parallelepiped

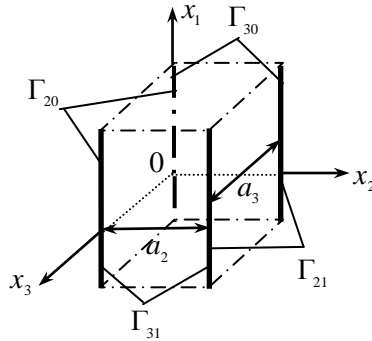


Figure 8: Unbounded parallelepiped with boundary strips Γ_{20} , Γ_{21} and Γ_{30} , Γ_{31} .

Problems (P3C) 8.1– (P3C) 8.16

To construct the Green's functions $G^{(j)}$, ($j=1-16$) of Poisson's equation $\nabla^2 G^{(j)}(x, \xi) = -\delta(x - \xi)$ for the unbounded parallelepiped $(-\infty \leq x_1 \leq \infty; 0 \leq x_2 \leq a_2; 0 \leq x_3 \leq a_3)$ under the following homogeneous boundary conditions:

Problem (P3C) 8.1

$$\begin{aligned} G^{(1)} &= 0; x_2 = 0; -\infty \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ G^{(1)} &= 0; x_2 = a_2; -\infty \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\ G^{(1)} &= 0; x_3 = 0; -\infty \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\ G^{(1)} &= 0; x_3 = a_3; -\infty \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 8.1 for unbounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 8.2

$$\begin{aligned} \partial G^{(2)} / \partial x_2 &= 0; x_2 = 0; -\infty \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\ \partial G^{(2)} / \partial x_2 &= 0; x_2 = a_2; -\infty \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial n_2' = g_2'(y_1, 0, y_3); \\ \partial G^{(2)} / \partial x_3 &= 0; x_3 = 0; -\infty \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\ \partial G^{(2)} / \partial x_3 &= 0; x_3 = a_3; -\infty \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, 0). \end{aligned}$$

The Answer to Problem (P3C) 8.2 for unbounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 8.3

$$\begin{aligned}
 G^{(3)} &= 0; x_2 = 0; -\infty \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \quad U = s_2(y_1, 0, y_3); \\
 G^{(3)} &= 0; x_2 = a_2; -\infty \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \quad U = s_2'(y_1, a_2, y_3); \\
 \partial G^{(3)} / \partial x_3 &= 0; x_3 = 0; -\infty \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \quad \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
 \partial G^{(3)} / \partial x_3 &= 0; x_3 = a_3; -\infty \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \quad \partial U / \partial n_3' = g_3'(y_1, y_2, 0).
 \end{aligned}$$

The Answer to Problem (P3C) 8.3 for unbounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 8.4

$$\begin{aligned}
 \partial G^{(4)} / \partial x_2 &= 0; x_2 = 0; -\infty \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \quad \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\
 \partial G^{(4)} / \partial x_2 &= 0; x_2 = a_2; -\infty \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \quad \partial U / \partial n_2' = g_2'(y_1, 0, y_3); \\
 G^{(4)} &= 0; x_3 = 0; -\infty \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \quad U = s_3(y_1, y_2, 0); \\
 G^{(4)} &= 0; x_3 = a_3; -\infty \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \quad U = s_3'(y_1, y_2, a_3).
 \end{aligned}$$

The Answer to Problem (P3C) 8.4 for unbounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 8.5

$$\begin{aligned}
 G^{(5)} &= 0; x_2 = 0, \quad -\infty \leq x_1 \leq \infty, \quad 0 \leq x_3 \leq a_3 \quad U = s_2(y_1, 0, y_3); \\
 \partial G^{(5)} / \partial x_2 &= 0; x_2 = a_2, -\infty \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \quad \partial U / \partial n_2' = g_2'(y_1, 0, y_3); \\
 G^{(5)} &= 0; x_3 = 0, a_3; -\infty \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \quad U = s_3(y_1, y_2, 0); \\
 G^{(5)} &= 0; x_3 = 0, a_3; -\infty \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \quad U = s_3'(y_1, y_2, a_3).
 \end{aligned}$$

The Answer to Problem (P3C) 8.5 for unbounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 8.6

$$\begin{aligned}
 \partial G^{(6)} / \partial x_2 &= 0; x_2 = 0, -\infty \leq x_1 \leq \infty, \quad 0 \leq x_3 \leq a_3; \quad \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\
 G^{(6)} &= 0; x_2 = a_2, -\infty \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \quad U = s_2'(y_1, a_2, y_3); \\
 \partial G^{(6)} / \partial x_3 &= 0; x_3 = 0, a_3; -\infty \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \quad \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
 \partial G^{(6)} / \partial x_3 &= 0; x_3 = 0, a_3; -\infty \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \quad \partial U / \partial n_3' = g_3'(y_1, y_2, 0).
 \end{aligned}$$

The Answer to Problem (P3C) 8.6 for unbounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 8.7

$$\begin{aligned}
 G^{(7)} &= 0; \quad x_2 = 0, \quad -\infty \leq x_1 \leq \infty, \quad 0 \leq x_3 \leq a_3; \quad U = s_2(y_1, 0, y_3); \\
 \partial G^{(7)} / \partial x_2 &= 0; \quad x_2 = a_2, \quad -\infty \leq x_1 \leq \infty, \quad 0 \leq x_3 \leq a_3; \quad \frac{\partial U}{\partial n_2'} = g_2'(y_1, 0, y_3); \\
 \partial G^{(7)} / \partial x_3 &= 0; \quad x_3 = 0, \quad a_3; \quad -\infty \leq x_1 \leq \infty, \quad 0 \leq x_2 \leq a_2; \quad \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
 \partial G^{(7)} / \partial x_3 &= 0; \quad x_3 = 0, \quad a_3; \quad -\infty \leq x_1 \leq \infty, \quad 0 \leq x_2 \leq a_2; \quad \partial U / \partial n_3' = g_3'(y_1, y_2, 0).
 \end{aligned}$$

The Answer to Problem (P3C) 8.7 for unbounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 8.8

$$\begin{aligned}
 \partial G^{(78)} / \partial x_2 &= 0; \quad x_2 = 0, \quad -\infty \leq x_1 \leq \infty, \quad 0 \leq x_3 \leq a_3; \quad \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\
 G^{(8)} &= 0; \quad x_2 = a_2, \quad -\infty \leq x_1 \leq \infty, \quad 0 \leq x_3 \leq a_3; \quad U = s_2'(y_1, a_2, y_3); \\
 G^{(8)} &= 0; \quad x_3 = 0, \quad a_3; \quad -\infty \leq x_1 \leq \infty, \quad 0 \leq x_2 \leq a_2; \quad U = s_3(y_1, y_2, 0); \\
 G^{(8)} &= 0; \quad x_3 = 0, \quad a_3; \quad -\infty \leq x_1 \leq \infty, \quad 0 \leq x_2 \leq a_2; \quad U = s_3'(y_1, y_2, a_3).
 \end{aligned}$$

The Answer to Problem (P3C) 8.8 for unbounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 8.9

$$\begin{aligned}
 G^{(9)} &= 0; \quad x_2 = 0, \quad a_2, \quad -\infty \leq x_1 \leq \infty, \quad 0 \leq x_3 \leq a_3; \quad U = s_2(y_1, 0, y_3); \\
 G^{(9)} &= 0; \quad x_2 = 0, \quad a_2, \quad -\infty \leq x_1 \leq \infty, \quad 0 \leq x_3 \leq a_3; \quad U = s_2'(y_1, a_2, y_3); \\
 \partial G^{(9)} / \partial x_3 &= 0; \quad x_3 = 0, \quad -\infty \leq x_1 \leq \infty, \quad 0 \leq x_2 \leq a_2; \quad \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
 G^{(9)} &= 0, \quad x_3 = a_3, \quad -\infty \leq x_1 \leq \infty, \quad 0 \leq x_2 \leq a_2; \quad U = s_3'(y_1, y_2, a_3).
 \end{aligned}$$

The Answer to Problem (P3C) 8.9 for unbounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 8.10

$$\begin{aligned}
 G^{(10)} &= 0; \quad x_2 = 0, \quad a_2, \quad -\infty \leq x_1 \leq \infty, \quad 0 \leq x_3 \leq a_3; \quad U = s_2(y_1, 0, y_3); \\
 G^{(10)} &= 0; \quad x_2 = 0, \quad a_2, \quad -\infty \leq x_1 \leq \infty, \quad 0 \leq x_3 \leq a_3; \quad U = s_2'(y_1, a_2, y_3); \\
 G^{(10)} &= 0; \quad x_3 = 0, \quad -\infty \leq x_1 \leq \infty, \quad 0 \leq x_2 \leq a_2; \quad U = s_3(y_1, y_2, 0); \\
 \partial G^{(10)} / \partial x_3 &= 0, \quad x_3 = a_3, \quad -\infty \leq x_1 \leq \infty, \quad 0 \leq x_2 \leq a_2; \quad \partial U / \partial n_3' = g_3'(y_1, y_2, 0).
 \end{aligned}$$

The Answer to Problem (P3C) 8.10 for unbounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 8.11

$$\begin{aligned} \partial G^{(11)}/\partial x_2 = 0; x_2 = 0; -\infty \leq x_1 \leq \infty, \quad 0 \leq x_3 \leq a_3; \partial U/\partial n_2 = g_2(y_1, 0, y_3); \\ \partial G^{(11)}/\partial x_2 = 0; x_2 = a_2; -\infty \leq x_1 \leq \infty, \quad 0 \leq x_3 \leq a_3; \partial U/\partial n_2' = g_2'(y_1, 0, y_3); \\ G^{(11)} = 0; x_3 = 0, -\infty \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\ \partial G^{(11)}/\partial x_3 = 0, x_3 = a_3, -\infty \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U/\partial n_3' = g_3'(y_1, y_2, 0). \end{aligned}$$

The Answer to Problem (P3C) 8.11 for unbounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 8.12

$$\begin{aligned} G^{(12)} = 0; x_2 = 0, -\infty \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ \partial G^{(11)}/\partial x_2 = 0; x_2 = a_2, -\infty \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U/\partial n_2' = g_2'(y_1, 0, y_3); \\ G^{(12)} = 0; x_3 = 0, -\infty \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\ \partial G^{(11)}/\partial x_3 = 0, x_3 = a_3, -\infty \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U/\partial n_3' = g_3'(y_1, y_2, 0). \end{aligned}$$

The Answer to Problem (P3C) 8.12 for unbounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates)

can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 8.13

$$\begin{aligned} \partial G^{(13)}/\partial x_3 = 0; x_2 = 0, -\infty \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U/\partial n_2 = g_2(y_1, 0, y_3); \\ G^{(13)} = 0; x_2 = a_2, -\infty \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\ G^{(13)} = 0; x_3 = 0, -\infty \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\ \partial G^{(13)}/\partial x_3 = 0, x_3 = a_3, -\infty \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U/\partial n_3' = g_3'(y_1, y_2, 0). \end{aligned}$$

The Answer to Problem (P3C) 8.13 for unbounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 8.14

$$\begin{aligned} \partial G^{(14)}/\partial x_2 = 0; x_2 = 0, a_2, -\infty \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U/\partial n_2 = g_2(y_1, 0, y_3); \\ \partial G^{(14)}/\partial x_2 = 0; x_2 = 0, a_2, -\infty \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U/\partial n_2' = g_2'(y_1, 0, y_3); \\ \partial G^{(14)}/\partial x_3 = 0; x_3 = 0, -\infty \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U/\partial n_3 = g_3(y_1, y_2, 0); \\ G^{(14)} = 0, \quad x_3 = a_3, \quad -\infty \leq x_1 \leq \infty, \quad 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 8.14 for unbounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 8.15

$$\begin{aligned}
 G^{(15)} &= 0; x_2 = 0, -\infty \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
 \partial G^{(15)} / \partial x_2 &= 0; x_2 = a_2, -\infty \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2'(y_1, 0, y_3); \\
 \partial G^{(15)} / \partial x_3 &= 0; x_3 = 0, -\infty \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
 G^{(15)} &= 0, x_3 = a_3, -\infty \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
 \end{aligned}$$

The Answer to Problem (P3C) 8.15 for unbounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 8.16

$$\begin{aligned}
 \partial G^{(16)} / \partial x_2 &= 0; x_2 = 0, -\infty \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\
 G^{(16)} &= 0; x_2 = a_2, -\infty \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
 \partial G^{(16)} / \partial x_3 &= 0; x_3 = 0, -\infty \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
 G^{(16)} &= 0, x_3 = a_3, -\infty \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
 \end{aligned}$$

The Answer to Problem (P3C) 8.16 for unbounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

(P3C)9. Semi-bounded Parallelepiped ($0 \leq x_1 \leq \infty; 0 \leq x_2 \leq a_2; 0 \leq x_3 \leq a_3$)

This section formulates thirty two boundary-value Problem (P3C) s on constructing Green's functions, $G^{(j)}$, ($j = 1 - 32$), of Poisson's equation for the semi-bounded parallelepiped

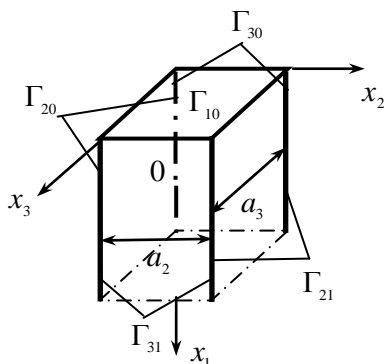


Figure 9: Semi-bounded parallelepiped with boundary half-strips $\Gamma_{20}, \Gamma_{21}, \Gamma_{30}, \Gamma_{31}$ and boundary rectangular Γ_{10} .

Problems (P3C) 9.1–(P3C)9.32

To construct the Green's functions $G^{(j)}(x, \xi)$, ($j=1-32$) of Poisson's equation $\nabla^2 G^{(j)}(x, \xi) = -\delta(x - \xi)$ for the semi-bounded parallelepiped ($0 \leq x_1 \leq \infty; 0 \leq x_2 \leq a_2; 0 \leq x_3 \leq a_3$) under the following homogeneous boundary conditions:

Problem (P3C) 9.1

$$\begin{aligned} G^{(1)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\ G^{(1)} &= 0; x_2 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ G^{(1)} &= 0; x_2 = a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\ G^{(1)} &= 0; x_3 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\ G^{(1)} &= 0; x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 9.1 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.2

$$\begin{aligned} \partial G^{(2)} / \partial x_1 &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\ \partial G^{(2)} / \partial x_2 &= 0; x_2 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\ \partial G^{(2)} / \partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial n_2' = g_2'(y_1, a_2, y_3); \\ \partial G^{(2)} / \partial x_3 &= 0; x_3 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\ \partial G^{(2)} / \partial x_3 &= 0; x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 9.2 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.3

$$\begin{aligned} G^{(3)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\ G^{(3)} &= 0; x_2 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ G^{(3)} &= 0; x_2 = a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\ \partial G^{(3)} / \partial x_3 &= 0; x_3 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\ \partial G^{(3)} / \partial x_3 &= 0; x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 9.3 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.4

$$\begin{aligned} \partial G^{(4)}/\partial x_1 &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U/\partial n_1 = g_1(0, y_2, y_3); \\ G^{(4)} &= 0; x_2 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ G^{(4)} &= 0; x_2 = a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\ \partial G^{(4)}/\partial x_3 &= 0; x_3 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U/\partial n_3 = g_3(y_1, y_2, 0); \\ \partial G^{(4)}/\partial x_3 &= 0; x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U/\partial n_3 = g_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 9.4 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.5

$$\begin{aligned} G^{(5)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\ \partial G^{(5)}/\partial x_2 &= 0; x_2 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U/\partial n_2 = g_2(y_1, 0, y_3); \\ \partial G^{(5)}/\partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U/\partial n_2' = g_2'(y_1, a_2, y_3); \\ G^{(5)} &= 0; x_3 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\ G^{(5)} &= 0; x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 9.5 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.6

$$\begin{aligned} \partial G^{(6)}/\partial x_1 &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U/\partial n_1 = g_1(0, y_2, y_3); \\ \partial G^{(6)}/\partial x_2 &= 0; x_2 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U/\partial n_2 = g_2(y_1, 0, y_3); \\ \partial G^{(6)}/\partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U/\partial n_2' = g_2'(y_1, a_2, y_3); \\ G^{(6)} &= 0; x_3 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\ G^{(6)} &= 0; x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 9.6 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.7

$$\begin{aligned} G^{(7)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\ G^{(7)} &= 0; x_2 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ \partial G^{(7)}/\partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U/\partial n_2' = g_2'(y_1, a_2, y_3); \\ G^{(7)} &= 0; x_3 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\ G^{(7)} &= 0; x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 9.7 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.8

$$\begin{aligned} \partial G^{(8)} / \partial x_1 = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\ G^{(8)} = 0; x_2 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ \partial G^{(8)} / \partial x_2 = 0; x_2 = a_2, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_2; \partial U / \partial n_2 = g_2'(y_1, a_2, y_3); \\ G^{(8)} = 0; x_3 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\ G^{(8)} = 0; x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 9.8 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.9

$$\begin{aligned} G^{(9)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\ \partial G^{(9)} / \partial x_2 = 0; x_2 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\ G^{(9)} = 0; x_2 = a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_2; U = s_2'(y_1, a_2, y_3); \\ \partial G^{(9)} / \partial x_3 = 0; x_3 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\ \partial G^{(9)} / \partial x_3 = 0; x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 9.9 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.10

$$\begin{aligned} \partial G^{(10)} / \partial x_1 = 0; x_1 = 0; 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\ \partial G^{(10)} / \partial x_2 = 0; x_2 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\ G^{(10)} = 0; x_2 = a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\ \partial G^{(10)} / \partial x_3 = 0; x_3 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\ \partial G^{(10)} / \partial x_3 = 0; x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 9.10 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.11

$$\begin{aligned}
G^{(11)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
G^{(11)} &= 0; x_2 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
\partial G^{(11)} / \partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2'(y_1, a_2, y_3); \\
\partial G^{(11)} / \partial x_3 &= 0; x_3 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
\partial G^{(11)} / \partial x_3 &= 0; x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 9.11 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.12

$$\begin{aligned}
\partial G^{(12)} / \partial x_1 &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\
G^{(12)} &= 0; x_2 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
\partial G^{(12)} / \partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2'(y_1, a_2, y_3); \\
\partial G^{(12)} / \partial x_3 &= 0; x_3 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
\partial G^{(12)} / \partial x_3 &= 0; x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 9.12 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.13

$$\begin{aligned}
G^{(13)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
\partial G^{(13)} / \partial x_2 &= 0; x_2 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\
G^{(13)} &= 0; x_2 = a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
G^{(13)} &= 0; x_3 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
G^{(13)} &= 0; x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 9.13 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.14

$$\begin{aligned}
\partial G^{(14)} / \partial x_1 &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\
\partial G^{(14)} / \partial x_2 &= 0; x_2 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\
G^{(14)} &= 0; x_2 = a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
G^{(14)} &= 0; x_3 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
G^{(14)} &= 0; x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 9.14 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.15

$$\begin{aligned}
 G^{(15)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
 G^{(15)} &= 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
 G^{(15)} &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
 \partial G^{(15)} / \partial x_3 &= 0; x_3 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3(y_1, y_2, 0); \\
 G^{(15)} &= 0; x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
 \end{aligned}$$

The Answer to Problem (P3C) 9.15 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.16

$$\begin{aligned}
 \partial G^{(16)} / \partial x_1 &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\
 G^{(16)} &= 0; x_2 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
 G^{(16)} &= 0; x_2 = a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
 \partial G^{(16)} / \partial x_3 &= 0; x_3 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, a_2, y_3); \\
 G^{(16)} &= 0; x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
 \end{aligned}$$

The Answer to Problem (P3C) 9.16 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.17

$$\begin{aligned}
 G^{(17)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
 G^{(17)} &= 0; x_2 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
 G^{(17)} &= 0; x_2 = a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
 G^{(17)} &= 0; x_3 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
 \partial G^{(17)} / \partial x_3 &= 0; x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, a_3).
 \end{aligned}$$

The Answer to Problem (P3C) 9.17 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.18

$$\begin{aligned} \partial G^{(18)}/\partial x_1 &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U/\partial n_1 = g_1(0, y_2, y_3); \\ G^{(18)} &= 0; x_2 = 0, a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ G^{(18)} &= 0; x_2 = 0, a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\ G^{(18)} &= 0; x_3 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\ \partial G^{(18)}/\partial x_3 &= 0; x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U/\partial n_3' = g_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 9.18 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.19

$$\begin{aligned} G^{(19)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\ \partial G^{(19)}/\partial x_2 &= 0; x_2 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U/\partial n_2 = g_2(y_1, 0, y_3); \\ \partial G^{(19)}/\partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U/\partial n_2' = g_2'(y_1, a_2, y_3); \\ G^{(19)} &= 0; x_3 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\ \partial G^{(19)}/\partial x_3 &= 0; x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U/\partial n_3' = g_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 9.19 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.20

$$\begin{aligned} \partial G^{(20)}/\partial x_1 &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U/\partial n_1 = g_1(0, y_2, y_3); \\ \partial G^{(20)}/\partial x_2 &= 0; x_2 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U/\partial n_2 = g_2(y_1, 0, y_3); \\ \partial G^{(20)}/\partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U/\partial n_2' = g_2'(y_1, a_2, y_3); \\ G^{(20)} &= 0; x_3 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\ \partial G^{(20)}/\partial x_3 &= 0; x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U/\partial n_3' = g_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 9.20 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.21

$$\begin{aligned} G^{(21)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\ G^{(21)} &= 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ \partial G^{(21)}/\partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U/\partial n_2' = g_2'(y_1, a_2, y_3); \\ G^{(21)} &= 0; x_3 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\ \partial G^{(21)}/\partial x_3 &= 0; x_3 = a_3, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U/\partial n_3' = g_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 9.21 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.22

$$\begin{aligned} \partial G^{(22)}/\partial x_1 = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U/\partial n_1 = g_1(0, y_2, y_3); \\ G^{(22)} = 0; x_2 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ \partial G^{(22)}/\partial x_2 = 0; x_2 = a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U/\partial n_2 = g_2'(y_1, a_2, y_3); \\ G^{(22)} = 0; x_3 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\ \partial G^{(22)}/\partial x_3 = 0; x_3 = a_3, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U/\partial n_3 = g_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 9.22 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.23

$$\begin{aligned} G^{(23)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\ \partial G^{(23)}/\partial x_2 = 0; x_2 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U/\partial n_2 = g_2(y_1, 0, y_3); \\ G^{(23)} = 0; x_2 = a_2, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\ G^{(23)} = 0; x_3 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\ \partial G^{(23)}/\partial x_3 = 0; x_3 = a_3, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U/\partial n_3 = g_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 9.23 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.24

$$\begin{aligned} \partial G^{(24)}/\partial x_1 = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U/\partial n_1 = g_1(0, y_2, y_3); \\ \partial G^{(24)}/\partial x_2 = 0; x_2 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U/\partial n_2 = g_2(y_1, 0, y_3); \\ G^{(24)} = 0; x_2 = a_2, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\ G^{(24)} = 0; x_3 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\ \partial G^{(24)}/\partial x_3 = 0; x_3 = a_3, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U/\partial n_3 = g_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 9.24 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.25

$$\begin{aligned}
G^{(25)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
\partial G^{(25)} / \partial x_2 &= 0; x_2 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\
\partial G^{(25)} / \partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial n_2' = g_2'(y_1, a_2, y_3); \\
\partial G^{(25)} / \partial x_3 &= 0; x_3 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
G^{(25)} &= 0; x_3 = a_3, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 9.25 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.26

$$\begin{aligned}
\partial G^{(26)} / \partial x_1 &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\
\partial G^{(26)} / \partial x_2 &= 0; x_2 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\
\partial G^{(26)} / \partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial n_2' = g_2'(y_1, a_2, y_3); \\
\partial G^{(26)} / \partial x_3 &= 0; x_3 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
G^{(26)} &= 0; x_3 = a_3, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 9.26 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.27

$$\begin{aligned}
G^{(27)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
G^{(27)} &= 0; x_2 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
\partial G^{(27)} / \partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2'(y_1, a_2, y_3); \\
\partial G^{(27)} / \partial x_3 &= 0; x_3 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
G^{(27)} &= 0; x_3 = a_3, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 9.27 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.28

$$\begin{aligned}
\partial G^{(28)} / \partial x_1 &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\
G^{(28)} &= 0; x_2 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
\partial G^{(28)} / \partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial n_2' = g_2'(y_1, a_2, y_3); \\
\partial G^{(28)} / \partial x_3 &= 0; x_3 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
G^{(28)} &= 0; x_3 = a_3, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 9.28 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.29

$$\begin{aligned}
 G^{(29)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
 \partial G^{(29)} / \partial x_2 &= 0; x_2 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\
 G^{(29)} &= 0; x_2 = a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
 \partial G^{(29)} / \partial x_3 &= 0; x_3 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
 G^{(29)} &= 0; x_3 = a_3, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
 \end{aligned}$$

The Answer to Problem (P3C) 9.29 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.30

$$\begin{aligned}
 \partial G^{(30)} / \partial x_1 &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\
 \partial G^{(30)} / \partial x_2 &= 0; x_2 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\
 G^{(30)} &= 0; x_2 = a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
 \partial G^{(30)} / \partial x_3 &= 0; x_3 = 0, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
 G^{(30)} &= 0; x_3 = a_3, 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
 \end{aligned}$$

The Answer to Problem (P3C) 9.30 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.31

$$\begin{aligned}
 \partial G^{(31)} / \partial x_1 &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\
 G^{(31)} &= 0; x_2 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
 G^{(31)} &= 0; x_2 = a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
 G^{(31)} &= 0; x_3 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
 G^{(31)} &= 0; x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, a_3).
 \end{aligned}$$

The Answer to Problem (P3C) 9.31 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 9.32

$$\begin{aligned}
 &G^{(32)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
 &\partial G^{(32)} / \partial x_2 = 0; x_2 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\
 &\partial G^{(32)} / \partial x_2 = 0; x_2 = a_2; 0 \leq x_1 \leq \infty, 0 \leq x_3 \leq a_3; \partial U / \partial n_2' = g_2'(y_1, a_2, y_3); \\
 &\partial G^{(32)} / \partial x_3 = 0; x_3 = 0; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
 &\partial G^{(32)} / \partial x_3 = 0; x_3 = a_3; 0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, a_3).
 \end{aligned}$$

The Answer to Problem (P3C) 9.32 for semi-bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

(P3C) 10. Bounded Parallelepiped ($0 \leq x_1 \leq a_1; 0 \leq x_2 \leq a_2; 0 \leq x_3 \leq a_3$)

This section formulates sixty four boundary-value Problem (P3C) s on constructing Green's functions, $G^{(j)}$, ($j = 1 - 64$), of Poisson's equation for the bounded parallelepiped

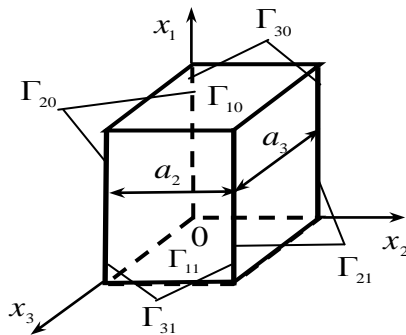


Figure 10: Bounded parallelepiped with boundary rectangular Γ_{10} , Γ_{11} , Γ_{20} , Γ_{21} and Γ_{30} , Γ_{31} .

Problems (P3C)10.1–(P3C)10.64

To construct the Green's functions $G^{(j)}(x, \xi)$, ($j = 1 - 64$) for Poisson's equation $\nabla^2 G^{(j)}(x, \xi) = -\delta(x - \xi)$ for the bounded parallelepiped ($0 \leq x_1 \leq a_1; 0 \leq x_2 \leq a_2; 0 \leq x_3 \leq a_3$) under the following homogeneous boundary conditions:

Problem (P3C) 10.1

$$\begin{aligned}
G^{(1)} &= 0; x_1 = 0; 0 \leq x_2 \leq a_2, \quad 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
G^{(1)} &= 0; x_1 = a_1; 0 \leq x_2 \leq a_2, \quad 0 \leq x_3 \leq a_3; U = s_1'(a_1, y_2, y_3); \\
G^{(1)} &= 0; x_2 = 0; 0 \leq x_1 \leq a_1, \quad 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
G^{(1)} &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, \quad 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
G^{(1)} &= 0; x_3 = 0; \quad 0 \leq x_1 \leq a_1, \quad 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
G^{(1)} &= 0; x_3 = a_3; \quad 0 \leq x_1 \leq a_1, \quad 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3);
\end{aligned}$$

The Answer to Problem (P3C) 10.1 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.2

$$\begin{aligned}
G^{(2)} &= 0; x_1 = 0; 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
G^{(2)} &= 0; x_1 = a_1; 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1'(a_1, y_2, y_3); \\
G^{(2)} &= 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
G^{(2)} &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
\partial G^{(2)} / \partial x_3 &= 0; x_3 = 0; \quad 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
\partial G^{(2)} / \partial x_3 &= 0; x_3 = a_3; \quad 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.2 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.3

$$\begin{aligned}
G^{(3)} &= 0; x_1 = 0; 0 \leq x_2 \leq a_2, \quad 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
G^{(3)} &= 0; x_1 = a_1; 0 \leq x_2 \leq a_2, \quad 0 \leq x_3 \leq a_3; U = s_1'(a_1, y_2, y_3); \\
G^{(3)} &= 0; x_2 = 0; 0 \leq x_1 \leq a_1, \quad 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
G^{(3)} &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, \quad 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
G^{(3)} &= 0; x_3 = 0; \quad 0 \leq x_1 \leq a_1, \quad 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
\partial G^{(3)} / \partial x_3 &= 0; x_3 = a_3; \quad 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.3 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.4

$$\begin{aligned}
G^{(4)} &= 0; x_1 = 0; 0 \leq x_2 \leq a_2, \quad 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
G^{(4)} &= 0; x_1 = a_1; 0 \leq x_2 \leq a_2, \quad 0 \leq x_3 \leq a_3; U = s_1'(a_1, y_2, y_3); \\
G^{(4)} &= 0; x_2 = 0; 0 \leq x_1 \leq a_1, \quad 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
G^{(4)} &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, \quad 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
\partial G^{(4)} / \partial x_3 &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_3, 0); \\
G^{(4)} &= 0; x_3 = a_3; 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.4 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.5

$$\begin{aligned}
\partial G^{(5)} / \partial x_1 &= 0; x_1 = 0, a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\
\partial G^{(5)} / \partial x_1 &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1' = g_1'(a_1, y_2, y_3); \\
\partial G^{(5)} / \partial x_2 &= 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\
\partial G^{(5)} / \partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2' = g_2'(y_1, a_2, y_3); \\
G^{(5)} &= 0; x_3 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
G^{(5)} &= 0; x_3 = a_3; 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.5 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.6

$$\begin{aligned}
\partial G^{(6)} / \partial x_1 &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\
\partial G^{(6)} / \partial x_1 &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1' = g_1'(a_1, y_2, y_3); \\
\partial G^{(6)} / \partial x_2 &= 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\
\partial G^{(6)} / \partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2' = g_2'(y_1, a_2, y_3); \\
G^{(6)} &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
\partial G^{(6)} / \partial x_3 &= 0; x_3 = a_3; 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, a_3)
\end{aligned}$$

The Answer to Problem (P3C) 10.6 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.7

$$\begin{aligned} \partial G^{(7)} / \partial x_1 = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\ \partial G^{(7)} / \partial x_1 = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1'(a_1, y_2, y_3); \\ \partial G^{(7)} / \partial x_2 = 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\ \partial G^{(7)} / \partial x_2 = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2'(y_1, a_2, y_3); \\ \partial G^{(7)} / \partial x_3 = 0; x_3 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\ \partial G^{(7)} / \partial x_3 = 0; x_3 = a_3; 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 10.7 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.8

$$\begin{aligned} \partial G^{(8)} / \partial x_1 = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\ \partial G^{(8)} / \partial x_1 = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1'(a_1, y_2, y_3); \\ \partial G^{(8)} / \partial x_2 = 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\ \partial G^{(8)} / \partial x_2 = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2'(y_1, a_2, y_3); \\ \partial G^{(8)} / \partial x_3 = 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\ G^{(8)} = 0; x_3 = a_3; 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 10.8 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.9

$$\begin{aligned} G^{(9)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\ G^{(9)} = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1'(a_1, y_2, y_3); \\ \partial G^{(9)} / \partial x_2 = 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\ \partial G^{(9)} / \partial x_2 = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2'(y_1, a_2, y_3); \\ G^{(9)} = 0; x_3 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\ G^{(9)} = 0; x_3 = a_3; 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3) \end{aligned}$$

The Answer to Problem (P3C) 10.9 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.10

$$\begin{aligned}
G^{(10)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
G^{(10)} &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1'(a_1, y_2, y_3); \\
\partial G^{(10)} / \partial x_2 &= 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\
\partial G^{(10)} / \partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2' = g_2'(y_1, a_2, y_3); \\
\partial G^{(10)} / \partial x_3 &= 0; x_3 = 0; 0 \leq x_1 \leq a_1, \quad 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
\partial G^{(10)} / \partial x_3 &= 0; x_3 = a_3; 0 \leq x_1 \leq a_1, \quad 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.10 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.11

$$\begin{aligned}
G^{(11)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
G^{(11)} &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1'(a_1, y_2, y_3); \\
\partial G^{(11)} / \partial x_2 &= 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\
\partial G^{(11)} / \partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2' = g_2'(y_1, a_2, y_3); \\
\partial G^{(11)} / \partial x_3 &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
G^{(11)} &= 0; x_3 = a_3; 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.11 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.12

$$\begin{aligned}
G^{(12)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
G^{(12)} &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1'(a_1, y_2, y_3); \\
\partial G^{(12)} / \partial x_2 &= 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\
\partial G^{(12)} / \partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2' = g_2'(y_1, a_2, y_3); \\
G^{(12)} &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
\partial G^{(12)} / \partial x_3 &= 0; x_3 = a_3; 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, a_3)
\end{aligned}$$

The Answer to Problem (P3C) 10.12 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.13

$$\begin{aligned}
& \partial G^{(13)} / \partial x_1 = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\
& \partial G^{(13)} / \partial x_1 = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1' = g_1'(a_1, y_2, y_3); \\
& G^{(13)} = 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
& G^{(13)} = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
& G^{(13)} = 0; x_3 = 0; 0 \leq x_1 \leq a_1, \quad 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
& G^{(13)} = 0; x_3 = a_3; 0 \leq x_1 \leq a_1, \quad 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.13 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.14

$$\begin{aligned}
& \partial G^{(14)} / \partial x_1 = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\
& \partial G^{(14)} / \partial x_1 = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1' = g_1'(a_1, y_2, y_3); \\
& G^{(14)} = 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
& G^{(14)} = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
& \partial G^{(14)} / \partial x_3 = 0; x_3 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
& \partial G^{(14)} / \partial x_3 = 0; x_3 = a_3; 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.14 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.15

$$\begin{aligned}
& \partial G^{(15)} / \partial x_1 = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\
& \partial G^{(15)} / \partial x_1 = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1' = g_1'(a_1, y_2, y_3); \\
& G^{(15)} = 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
& G^{(15)} = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
& G^{(15)} = 0; x_3 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
& \partial G^{(15)} / \partial x_3 = 0; x_3 = a_3; 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.15 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.16

$$\begin{aligned}
& \partial G^{(16)} / \partial x_1 = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\
& \partial G^{(16)} / \partial x_1 = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1' = g_1'(a_1, y_2, y_3); \\
& \quad G^{(16)} = 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
& \quad G^{(16)} = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
& \partial G^{(16)} / \partial x_3 = 0; x_3 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
& \quad G^{(16)} = 0; x_3 = a_3; 0 \leq x_1 \leq a_1, \quad 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.16 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.17

$$\begin{aligned}
& G^{(17)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
& \partial G^{(17)} / \partial x_1 = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1' = g_1'(a_1, y_2, y_3); \\
& \quad G^{(17)} = 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
& \quad G^{(17)} = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
& \quad G^{(17)} = 0; x_3 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
& \quad G^{(17)} = 0; x_3 = a_3; 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.17 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.18

$$\begin{aligned}
& G^{(18)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
& \partial G^{(18)} / \partial x_1 = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1' = g_1'(a_1, y_2, y_3); \\
& \quad G^{(18)} = 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
& \quad G^{(18)} = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
& \partial G^{(18)} / \partial x_3 = 0; x_3 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
& \partial G^{(18)} / \partial x_3 = 0; x_3 = a_3; 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.18 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.19

$$\begin{aligned}
&G^{(19)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
&\partial G^{(19)} / \partial x_1 = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1' = g_1'(a_1, y_2, y_3); \\
&G^{(19)} = 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
&G^{(19)} = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
&G^{(19)} = 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
&\partial G^{(19)} / \partial x_3 = 0; x_3 = a_3; 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.19 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.20

$$\begin{aligned}
&G^{(20)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
&\partial G^{(20)} / \partial x_1 = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1' = g_1'(a_1, y_2, y_3); \\
&G^{(20)} = 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
&G^{(20)} = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
&\partial G^{(20)} / \partial x_3 = 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_3, 0); \\
&G^{(20)} = 0; x_3 = a_3; 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.20 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.21

$$\begin{aligned}
&\partial G^{(21)} / \partial x_1 = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\
&G^{(21)} = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
&\partial G^{(21)} / \partial x_2 = 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\
&\partial G^{(21)} / \partial x_2 = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2' = g_2'(y_1, a_2, y_3); \\
&G^{(21)} = 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
&G^{(21)} = 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.21 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.22

$$\begin{aligned} \partial G^{(22)} / \partial x_1 = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\ G^{(22)} = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ \partial G^{(22)} / \partial x_2 = 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\ \partial G^{(22)} / \partial x_2 = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2' = g_2'(y_1, a_2, y_3); \\ \partial G^{(22)} / \partial x_3 = 0; x_3 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\ \partial G^{(22)} / \partial x_3 = 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 10.22 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.23

$$\begin{aligned} \partial G^{(23)} / \partial x_1 = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\ G^{(23)} = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ \partial G^{(23)} / \partial x_2 = 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\ \partial G^{(23)} / \partial x_2 = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2' = g_2'(y_1, a_2, y_3); \\ G^{(23)} = 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\ \partial G^{(23)} / \partial x_3 = 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 10.23 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.24

$$\begin{aligned} \partial G^{(24)} / \partial x_1 = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\ G^{(24)} = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ \partial G^{(24)} / \partial x_2 = 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\ \partial G^{(24)} / \partial x_2 = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2' = g_2'(y_1, a_2, y_3); \\ \partial G^{(24)} / \partial x_3 = 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\ G^{(24)} = 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 10.24 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.25

$$\begin{aligned}
G^{(25)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
\partial G^{(25)} / \partial x_1 &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1' = g_1'(a_1, y_2, y_3); \\
\partial G^{(25)} / \partial x_2 &= 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2' = g_2'(y_1, 0, y_3); \\
\partial G^{(25)} / \partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2' = g_2'(y_1, a_2, y_3); \\
G^{(25)} &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
G^{(25)} &= 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.25 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.26

$$\begin{aligned}
G^{(26)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
\partial G^{(26)} / \partial x_1 &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1' = g_1'(a_1, y_2, y_3); \\
\partial G^{(26)} / \partial x_2 &= 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2' = g_2'(y_1, 0, y_3); \\
\partial G^{(26)} / \partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2' = g_2'(y_1, a_2, y_3); \\
\partial G^{(26)} / \partial x_3 &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, 0); \\
\partial G^{(26)} / \partial x_3 &= 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.26 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.27

$$\begin{aligned}
G^{(27)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
\partial G^{(27)} / \partial x_1 &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1' = g_1'(a_1, y_2, y_3); \\
\partial G^{(27)} / \partial x_2 &= 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2' = g_2'(y_1, 0, y_3); \\
\partial G^{(27)} / \partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2' = g_2'(y_1, a_2, y_3); \\
G^{(27)} &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
\partial G^{(27)} / \partial x_3 &= 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.27 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.28

$$\begin{aligned}
&G^{(28)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
&\partial G^{(28)} / \partial x_1 = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1' = g_1'(a_1, y_2, y_3); \\
&\partial G^{(28)} / \partial x_2 = 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\
&\partial G^{(28)} / \partial x_2 = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2' = g_2'(y_1, a_2, y_3); \\
&\partial G^{(28)} / \partial x_3 = 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
&G^{(28)} = 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.28 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.29

$$\begin{aligned}
&\partial G^{(29)} / \partial x_1 = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\
&G^{(29)} = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
&G^{(29)} = 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
&G^{(29)} = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
&G^{(29)} = 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
&G^{(29)} = 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.29 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.30

$$\begin{aligned}
&\partial G^{(30)} / \partial x_1 = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\
&G^{(30)} = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
&G^{(30)} = 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
&G^{(30)} = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
&\partial G^{(30)} / \partial x_3 = 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
&\partial G^{(30)} / \partial x_3 = 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.30 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.31

$$\begin{aligned}
&\partial G^{(31)}/\partial x_1 = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U/\partial n_1 = g_1(0, y_2, y_3); \\
&G^{(31)} = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
&G^{(31)} = 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
&G^{(31)} = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
&G^{(31)} = 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
&\partial G^{(31)}/\partial x_3 = 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U/\partial n_3 = g_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.31 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.32

$$\begin{aligned}
&\partial G^{(32)}/\partial x_1 = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U/\partial n_1 = g_1(0, y_2, y_3); \\
&G^{(32)} = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
&G^{(32)} = 0; x_2 = 0; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
&G^{(32)} = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
&\partial G^{(32)}/\partial x_3 = 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U/\partial n_3 = g_3(y_1, y_2, 0); \\
&G^{(32)} = 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.32 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.33

$$\begin{aligned}
&G^{(33)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
&G^{(33)} = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
&\partial G^{(33)}/\partial x_2 = 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U/\partial n_2 = g_2(y_1, 0, y_3); \\
&G^{(33)} = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
&G^{(33)} = 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
&G^{(33)} = 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.33 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.34

$$\begin{aligned}
G^{(34)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
G^{(34)} &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
\partial G^{(34)} / \partial x_2 &= 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\
G^{(34)} &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
\partial G^{(34)} / \partial x_3 &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
\partial G^{(34)} / \partial x_3 &= 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.34 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.35

$$\begin{aligned}
G^{(35)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
G^{(35)} &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
\partial G^{(35)} / \partial x_2 &= 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\
G^{(35)} &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
G^{(35)} &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
\partial G^{(35)} / \partial x_3 &= 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.35 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.36

$$\begin{aligned}
G^{(36)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
G^{(36)} &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
\partial G^{(36)} / \partial x_2 &= 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\
G^{(36)} &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
\partial G^{(36)} / \partial x_3 &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
G^{(36)} &= 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.36 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.37

$$\begin{aligned}
G^{(37)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
G^{(37)} &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
G^{(37)} &= 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
\partial G^{(37)} / \partial x_2 &= 0; x_2 = a_2, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n'_2 = g'_2(y_1, a_2, y_3); \\
G^{(37)} &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
G^{(37)} &= 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s'_3(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.37 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.38

$$\begin{aligned}
G^{(38)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
G^{(38)} &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
G^{(38)} &= 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
\partial G^{(38)} / \partial x_2 &= 0; x_2 = a_2, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n'_2 = g'_2(y_1, a_2, y_3); \\
\partial G^{(38)} / \partial x_3 &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n'_3 = g'_3(y_1, y_2, 0); \\
\partial G^{(38)} / \partial x_3 &= 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n'_3 = g'_3(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.38 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.39

$$\begin{aligned}
G^{(39)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
G^{(39)} &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
G^{(39)} &= 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
\partial G^{(39)} / \partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n'_3 = g'_2(y_1, a_2, y_3); \\
G^{(39)} &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
\partial G^{(39)} / \partial x_3 &= 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n'_3 = g'_3(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.39 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.40

$$\begin{aligned}
G^{(40)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
G^{(40)} &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
G^{(40)} &= 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
\partial G^{(40)} / \partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n'_2 = g'_2(y_1, a_2, y_3); \\
\partial G^{(40)} / \partial x_3 &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n'_3 = g'_3(y_1, y_2, 0); \\
G^{(40)} &= 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s'_3(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.40 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.41

$$\begin{aligned}
\partial G^{(41)} / \partial x_1 &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n'_1 = g'_1(0, y_2, y_3); \\
\partial G^{(41)} / \partial x_1 &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n'_1 = g'_1(a_1, y_2, y_3); \\
G^{(41)} &= 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
\partial G^{(41)} / \partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n'_2 = g'_2(y_1, a_2, y_3); \\
G^{(41)} &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
G^{(41)} &= 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s'_3(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.41 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.42

$$\begin{aligned}
\partial G^{(42)} / \partial x_1 &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n'_1 = g'_1(0, y_2, y_3); \\
\partial G^{(42)} / \partial x_1 &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n'_1 = g'_1(a_1, y_2, y_3); \\
G^{(42)} &= 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
\partial G^{(42)} / \partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n'_2 = g'_2(y_1, a_2, y_3); \\
\partial G^{(42)} / \partial x_3 &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n'_3 = g'_3(y_1, y_2, 0); \\
\partial G^{(42)} / \partial x_3 &= 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n'_3 = g'_3(y_1, y_2, a_3)
\end{aligned}$$

The Answer to Problem (P3C) 10.42 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.43

$$\begin{aligned}
& \partial G^{(43)} / \partial x_1 = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\
& \partial G^{(43)} / \partial x_1 = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1' = g_1'(a_1, y_2, y_3); \\
& \quad G^{(43)} = 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
& \partial G^{(43)} / \partial x_2 = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2' = g_2'(y_1, a_2, y_3); \\
& \quad G^{(43)} = 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
& \partial G^{(43)} / \partial x_3 = 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.43 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.44

$$\begin{aligned}
& \partial G^{(44)} / \partial x_1 = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\
& \partial G^{(44)} / \partial x_1 = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1' = g_1'(a_1, y_2, y_3); \\
& \quad G^{(44)} = 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
& \partial G^{(44)} / \partial x_2 = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2' = g_2'(y_1, a_2, y_3); \\
& \quad \partial G^{(44)} / \partial x_3 = 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
& \quad G^{(44)} = 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.44 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.45

$$\begin{aligned}
& G^{(45)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
& \partial G^{(45)} / \partial x_1 = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1' = g_1'(a_1, y_2, y_3); \\
& \quad G^{(45)} = 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
& \partial G^{(45)} / \partial x_2 = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2' = g_2'(y_1, a_2, y_3); \\
& \quad G^{(45)} = 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
& \quad G^{(45)} = 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.45 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.46

$$\begin{aligned}
&G^{(46)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
&\partial G^{(46)} / \partial x_1 = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n'_1 = g'_1(a_1, y_2, y_3); \\
&G^{(46)} = 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
&\partial G^{(46)} / \partial x_2 = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n'_2 = g'_2(y_1, a_2, y_3); \\
&\partial G^{(46)} / \partial x_3 = 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n'_3 = g'_3(y_1, y_2, 0); \\
&\partial G^{(46)} / \partial x_3 = 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n'_3 = g'_3(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.46 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.47

$$\begin{aligned}
&G^{(47)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
&\partial G^{(47)} / \partial x_1 = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n'_1 = g'_1(a_1, y_2, y_3); \\
&G^{(47)} = 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
&\partial G^{(47)} / \partial x_2 = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n'_2 = g'_2(y_1, a_2, y_3); \\
&G^{(47)} = 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
&\partial G^{(47)} / \partial x_3 = 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n'_3 = g'_3(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.47 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.48

$$\begin{aligned}
&G^{(48)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
&\partial G^{(48)} / \partial x_1 = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n'_1 = g'_1(a_1, y_2, y_3); \\
&G^{(48)} = 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\
&\partial G^{(48)} / \partial x_2 = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n'_2 = g'_2(y_1, a_2, y_3); \\
&\partial G^{(48)} / \partial x_3 = 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n'_3 = g'_3(y_1, y_2, 0); \\
&G^{(48)} = 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s'_3(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.48 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.49

$$\begin{aligned} \partial G^{(49)} / \partial x_1 &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\ G^{(49)} &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ G^{(49)} &= 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ \partial G^{(49)} / \partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_3 = g_2'(y_1, a_2, y_3); \\ G^{(49)} &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\ G^{(49)} &= 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 10.49 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) a 10.50

$$\begin{aligned} \partial G^{(50)} / \partial x_1 &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\ G^{(50)} &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ G^{(50)} &= 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ \partial G^{(50)} / \partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2' = g_2'(y_1, a_2, y_3); \\ \partial G^{(50)} / \partial x_3 &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\ \partial G^{(50)} / \partial x_3 &= 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 10.50 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.51

$$\begin{aligned} \partial G^{(51)} / \partial x_1 &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\ G^{(51)} &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ G^{(51)} &= 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ \partial G^{(51)} / \partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2' = g_2'(y_1, a_2, y_3); \\ G^{(51)} &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\ \partial G^{(51)} / \partial x_3 &= 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 10.51 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.52

$$\begin{aligned} \partial G^{(52)} / \partial x_1 &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\ G^{(52)} &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ G^{(52)} &= 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ \partial G^{(52)} / \partial x_2 &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2'(y_1, a_2, y_3); \\ \partial G^{(52)} / \partial x_3 &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\ G^{(52)} &= 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 10.52 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.53

$$\begin{aligned} \partial G^{(53)} / \partial x_1 &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\ \partial G^{(53)} / \partial x_1 &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1'(a_1, y_2, y_3); \\ \partial G^{(53)} / \partial x_2 &= 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\ G^{(53)} &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\ G^{(53)} &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\ G^{(53)} &= 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 10.53 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.54

$$\begin{aligned} \partial G^{(54)} / \partial x_1 &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\ \partial G^{(54)} / \partial x_1 &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1'(a_1, y_2, y_3); \\ \partial G^{(54)} / \partial x_2 &= 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\ G^{(54)} &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\ \partial G^{(54)} / \partial x_3 &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\ \partial G^{(54)} / \partial x_3 &= 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 10.54 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.55

$$\begin{aligned}
& \partial G^{(55)} / \partial x_1 = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\
& \partial G^{(55)} / \partial x_1 = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1' = g_1'(a_1, y_2, y_3); \\
& \partial G^{(55)} / \partial x_2 = 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\
& \quad G^{(55)} = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
& \quad G^{(55)} = 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
& \partial G^{(55)} / \partial x_3 = 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.55 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.56

$$\begin{aligned}
& \partial G^{(56)} / \partial x_1 = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\
& \partial G^{(56)} / \partial x_1 = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1' = g_1'(a_1, y_2, y_3); \\
& \partial G^{(56)} / \partial x_2 = 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\
& \quad G^{(56)} = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
& \partial G^{(56)} / \partial x_3 = 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
& \quad G^{(56)} = 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.56 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.57

$$\begin{aligned}
& G^{(57)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
& \partial G^{(57)} / \partial x_1 = 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1' = g_1'(a_1, y_2, y_3); \\
& \partial G^{(57)} / \partial x_2 = 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\
& \quad G^{(57)} = 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
& \quad G^{(57)} = 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
& \quad G^{(57)} = 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.57 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.58

$$\begin{aligned}
G^{(58)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
\partial G^{(58)} / \partial x_1 &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1' = g_1'(a_1, y_2, y_3); \\
\partial G^{(58)} / \partial x_2 &= 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\
G^{(58)} &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
\partial G^{(58)} / \partial x_3 &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
\partial G^{(58)} / \partial x_3 &= 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.58 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.59

$$\begin{aligned}
G^{(59)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
\partial G^{(59)} / \partial x_1 &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1' = g_1'(a_1, y_2, y_3); \\
\partial G^{(59)} / \partial x_2 &= 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\
G^{(59)} &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
G^{(59)} &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\
\partial G^{(59)} / \partial x_3 &= 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.59 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.60

$$\begin{aligned}
G^{(60)} &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_1(0, y_2, y_3); \\
\partial G^{(60)} / \partial x_1 &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1' = g_1'(a_1, y_2, y_3); \\
\partial G^{(60)} / \partial x_2 &= 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\
G^{(60)} &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\
\partial G^{(60)} / \partial x_3 &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\
G^{(60)} &= 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3).
\end{aligned}$$

The Answer to Problem (P3C) 10.60 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.61

$$\begin{aligned} \partial G^{(61)} / \partial x_1 &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\ G^{(61)} &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ \partial G^{(61)} / \partial x_2 &= 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\ G^{(61)} &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\ G^{(61)} &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\ G^{(61)} &= 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 10.61 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.62

$$\begin{aligned} \partial G^{(62)} / \partial x_1 &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\ G^{(62)} &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ \partial G^{(62)} / \partial x_2 &= 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\ G^{(62)} &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\ \partial G^{(62)} / \partial x_3 &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\ \partial G^{(62)} / \partial x_3 &= 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 10.62 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.63

$$\begin{aligned} \partial G^{(63)} / \partial x_1 &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\ G^{(63)} &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ \partial G^{(63)} / \partial x_2 &= 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\ G^{(63)} &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\ G^{(63)} &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3(y_1, y_2, 0); \\ \partial G^{(63)} / \partial x_3 &= 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3' = g_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 10.63 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

Problem (P3C) 10.64

$$\begin{aligned} \partial G^{(64)} / \partial x_1 &= 0; x_1 = 0, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; \partial U / \partial n_1 = g_1(0, y_2, y_3); \\ G^{(64)} &= 0; x_1 = a_1, 0 \leq x_2 \leq a_2, 0 \leq x_3 \leq a_3; U = s_2(y_1, 0, y_3); \\ \partial G^{(64)} / \partial x_2 &= 0; x_2 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_3 \leq a_3; \partial U / \partial n_2 = g_2(y_1, 0, y_3); \\ G^{(64)} &= 0; x_2 = a_2; 0 \leq x_1 \leq a_1, \quad 0 \leq x_3 \leq a_3; U = s_2'(y_1, a_2, y_3); \\ \partial G^{(64)} / \partial x_3 &= 0; x_3 = 0, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; \partial U / \partial n_3 = g_3(y_1, y_2, 0); \\ G^{(64)} &= 0; x_3 = a_3, 0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2; U = s_3'(y_1, y_2, a_3). \end{aligned}$$

The Answer to Problem (P3C) 10.64 for bounded parallelepiped (Green's function for Poisson's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)