

# LIST OF THE BOUNDARY-VALUE Problems (L2C) FOR 2D CARTESIAN DOMAINS, FOR WHICH THE GREEN'S TENSORS HAVE BEEN DERIVED

All these Green's tensors can be found in the book:

Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton  
and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

It is important to notice that all the results given in this file, with the exception of the results concerning the solutions for boundary-value Problem (L2Cs) for the rectangle are given in extremely compact form in terms of elementary functions. In the case of the rectangular domain the obtained results are given in the form of a sum of elementary functions consisted of the singular parts of the solution and ordinary infinite series comprising exponential, trigonometric and hyperbolic functions. Moreover, it can be said that the list of expressions for dilatation influence functions and Green's matrices for Lamé's equations are presented in a compact form. This form contains some derivatives of the respective Green's functions for Poisson's equation.

## (L2C) 1. Plane ( $-\infty \leq x_1, x_2 \leq \infty$ )

Section 1 gives the functions of influence of the unit concentrated body forces  $\int_V \delta_{ik} \delta(x - \xi) dV(\xi) = \delta_{ik}$ ,  $i, k=1,2$ , applied at the inner plane points  $\xi \equiv (\xi_1, \xi_2)$  along co-ordinate axis  $0x_k$ , onto the bulk dilatation (the influence functions for the dilatation  $-\Theta^{(k)}(x, \xi)$ ) as well as onto the displacements (the components of the displacements Green's matrix  $-U_i^{(k)}(x, \xi)$  at the points of observation  $x \equiv (x_1, x_2)$  along co-ordinate axis  $0x_i$ . The formulations to this boundary-value Problem (L2C) on constructing the influence functions for dilatation and Green's matrices for Lamé's equations are given there.

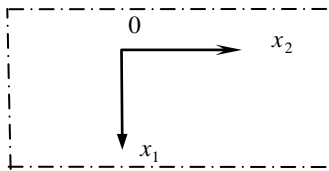


Figure 1: Plane in Cartesian co-ordinates.

**Problem (L2C) 1.1** To construct the functions describing the influence of the unit concentrated body forces  $\int_V \delta_{ik} \delta(x-\xi) dV(\xi) = \delta_{ik}$ ;  $i, k=1,2$  applied to the inner point's  $\xi \equiv (\xi_1, \xi_2)$  of the plane along the co-ordinate axis  $0x_k$  onto the bulk dilatation (the influence function for the dilatation being- $\Theta^{(k)}(x, \xi)$ ) as well as onto the displacements (the components of the displacements Green's matrix- $U_i^{(k)}(x, \xi)$ ) at the points of observation  $x \equiv (x_1, x_2)$  along the co-ordinate axis  $0x_i$ .

To solve the Problem (L2C) it is necessary to integrate the set of Lamé's equations

$$\nabla^2 U_i^{(k)}(x, \xi) + (\lambda + \mu) \Theta_{,i}^{(k)}(x, \xi) = -\delta_{ik} \delta(x - \xi).$$

**The Answer to Problem (L2C) 1.1 for plane** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

**(L2C) 2. Half-plane** ( $0 \leq x_1 \leq \infty, -\infty \leq x_2 \leq \infty$ )

Section 2 gives the functions of influence of the unit concentrated body forces  $\int_V \delta_{ik} \delta(x-\xi) dV(\xi) = \delta_{ik}$ ,  $i, k=1,2$ , applied at the inner half-plane points  $\xi \equiv (\xi_1, \xi_2)$  along co-ordinate axis  $0x_k$ , onto the bulk dilatation (the influence functions for the dilatation- $\Theta^{(k)}(x, \xi)$ ) as well as onto the displacements (the components of the displacements Green's matrix- $U_i^{(k)}(x, \xi)$ ) at the points of observation  $x \equiv (x_1, x_2)$  along co-ordinate axis  $0x_i$ . The formulations to four boundary-value Problem (L2C)s on constructing the influence functions for dilatation and Green's matrices for Lamé's equations in a case of the half-plane are given there.

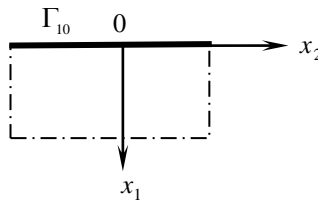


Figure 2: Half-plane with the boundary straight line  $\Gamma_{10}$ .

## Problems (L2C) of First Type. Problems (L2C) 2.1 and (L2C) 2.2

To construct the influence functions for the dilatation- $\Theta^{(k)}(x, \xi)$  and the components for the displacements Green's matrix- $U_i^{(k)}(x, \xi)$  for Lamé's equations for the elastic half-plane ( $0 \leq x_1 \leq \infty, -\infty \leq x_2 \leq \infty$ ) at the following locally mixed boundary conditions for the sliding-type fixation

### Problem (L2C) 2.1

$$U_1^{(k)} = \sigma_{12}^{(k)} = 0; x_1 = 0, -\infty \leq x_2 \leq \infty.$$

The Answer to Problem (L2C) 2.1 for half-plane (Green's tensor The Answer to for Lamé's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

### Problem (L2C) 2.2

$$\sigma_{11}^{(k)} = U_2^{(k)} = 0; x_1 = 0, -\infty \leq x_2 \leq \infty.$$

The Answer to Problem (L2C) 2.2 for half-plane (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

**Problem (L2C) of Second Type.** To construct the influence function for the dilatation- $\Theta^{(k)}(x, \xi)$  and the components of the displacements Green's matrix  $U_i^{(k)}(x, \xi)$  for Lamé's equation for the elastic half plane ( $0 \leq x_1 \leq \infty, -\infty \leq x_2 \leq \infty$ ) under the following boundary conditions for a rigid-type fixation

### Problem (L2C) 2.3

$$U_1^{(k)} = U_2^{(k)} = 0; x_1 = 0; -\infty \leq x_2 \leq \infty.$$

The Answer to Problem (L2C) 2.3 for half-plane (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

**Problem (L2C) of Third Type.**

To construct the influence function for the dilatation  $\Theta^{(k)}(x, \xi)$  and for the components of the displacements Green's matrix  $-U_i^{(k)}(x, \xi)$  for Lamé's equations for the elastic half-plane ( $0 \leq x_1 \leq \infty, -\infty \leq x_2 \leq \infty$ ) with the free boundary straight line, i.e. under the following boundary conditions

**Problem (L2C) 2.4**  $\sigma_{11}^{(k)} = \sigma_{12}^{(k)} = 0; x_1 = 0, \quad -\infty \leq x_2 \leq \infty.$

The Answer to Problem (L2C) 2.4 for half-plane (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

**(L2C) 3. Quadrant ( $0 \leq x_1, x_2 \leq \infty$ )**

Section 3 gives the functions of influence of the unit concentrated body forces  $\int_V \delta_{ik} \delta(x - \xi) dV(\xi) = \delta_{ik}, \quad i, k=1,2,$  applied at the inner quadrant points  $\xi \equiv (\xi_1, \xi_2)$  along co-ordinate axis  $0x_k$ , onto the bulk dilatation (the influence functions for the dilatation  $\Theta^{(k)}(x, \xi)$ ) as well as onto the displacements (the components of the displacements Green's matrix  $-U_i^{(k)}(x, \xi)$ ) at the points of observation  $x \equiv (x_1, x_2)$  along co-ordinate axis  $0x_i$ . The formulations and the final Answers to eight boundary-value Problem (L2C)s on constructing the influence functions for dilatation and Green's matrices for Lamé's equations in the case of the quadrant are given there.

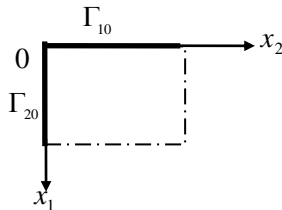


Figure 3: Quadrant with boundary half-straight lines  $\Gamma_{10}$  and  $\Gamma_{20}$ .

**Problems (L2C) of First Type. Problem (L2C) 3.1 to L2C) 3.4**

To construct influence functions for the dilatation  $\Theta^{(k)}(x, \xi)$  and for components of the displacements Green's matrix  $U_i^{(k)}(x, \xi)$  for Lamé's equation for the

elastic ( $0 \leq x_1 \leq \infty$ ,  $0 \leq x_2 \leq \infty$ ) under the following locally mixed boundary conditions of a sliding-fixation type.

**Problem (L2C) 3.1**

$$\sigma_{11}^{(k)} = U_2^{(k)} = 0; x_1 = 0, 0 \leq x_2 \leq \infty; \quad \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = 0, 0 \leq x_1 \leq \infty.$$

The Answer to Problem (L2C) 3.1 for quadrant (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
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**Problem (L2C) 3.2**

$$U_1^{(k)} = \sigma_{12}^{(k)} = 0; x_1 = 0, 0 \leq x_2 \leq \infty; \quad U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = 0, 0 \leq x_1 \leq \infty.$$

The Answer to Problem (L2C) 3.2 for quadrant (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
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**Problem (L2C) 3.3**

$$U_1^{(k)} = \sigma_{12}^{(k)} = 0; x_1 = 0, 0 \leq x_2 \leq \infty; \quad \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = 0, 0 \leq x_1 \leq \infty.$$

The Answer to Problem (L2C) 3.3 for quadrant (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
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**Problem (L2C) 3.4**

$$\sigma_{11}^{(k)} = U_2^{(k)} = 0; x_1 = 0, 0 \leq x_2 \leq \infty; \quad U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = 0, 0 \leq x_1 \leq \infty.$$

The Answer to Problem (L2C) 3.4 for quadrant (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
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**Problem (L2C) of Second Type. Problems (L2C) 3.5 and 3.6**

To construct influence functions for the dilatation- $\Theta^{(k)}(x, \xi)$  and for the components of the displacement Green's matrix  $-U_i^{(k)}(x, \xi)$  for Lamé's equations for the elastic quadrant ( $0 \leq x_1 \leq \infty$ ,  $0 \leq x_2 \leq \infty$ ) under the following mixed boundary conditions: the rigid on-the boundary straight line

$(x_1 = 0, 0 \leq x_2 \leq \infty)$ , type and fixations of a sliding type on the boundary straight line  $(x_2 = 0, 0 \leq x_1 \leq \infty)$ .

**Problem (L2C) 3.5**

$$U_1^{(k)} = U_2^{(k)} = 0; x_1 = 0, 0 \leq x_2 \leq \infty; \quad \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = 0, 0 \leq x_1 \leq \infty.$$

The Answer to Problem (L2C) 3.5 for quadrant (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:

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**Problem (L2C) 3.6**

$$U_1^{(k)} = U_2^{(k)} = 0; x_1 = 0, 0 \leq x_2 \leq \infty; \quad U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = 0, 0 \leq x_1 \leq \infty.$$

The Answer to Problem (L2C) 3.6 for quadrant (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:

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**Problems (L2C) of Third Type. Problems (L2C) 3.7 and L2C 3.8**

To construct the influence functions for the dilatation  $\Theta^{(k)}(x, \xi)$  and for the components of the displacements Green's matrix  $-U_i^{(k)}(x, \xi)$  of Lamé's equation for the elastic quadrant  $(0 \leq x_1, x_2 \leq \infty)$  under the following mixed boundary conditions: a type of the free boundary straight line  $(x_1 = 0, 0 \leq x_2 \leq \infty)$ , and a type of a sliding fixation at the boundary straight line  $(x_2 = 0, 0 \leq x_1 \leq \infty)$ .

**Problem (L2C) 3.7**

$$\sigma_{11}^{(k)} = \sigma_{12}^{(k)} = 0; x_1 = 0, 0 \leq x_2 \leq \infty; \quad \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = 0, 0 \leq x_1 \leq \infty.$$

The Answer to Problem (L2C) 3.7 for quadrant (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:

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**Problem (L2C) 3.8**

$$\sigma_{11}^{(k)} = \sigma_{12}^{(k)} = 0; x_1 = 0, 0 \leq x_2 \leq \infty; \quad U_2^{(k)} = \sigma_{22}^{(k)} = 0; x_2 = 0, 0 \leq x_1 \leq \infty.$$

**The Answer to Problem (L2C) 3.8 for quadrant** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

**(L2C) 4. Strip** ( $-\infty \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2$ )

Section 4 gives the functions of influence of the unit concentrated body forces  $\int_V \delta_{ik} \delta(x - \xi) dV(\xi) = \delta_{ik}$ ,  $i, k=1,2$ , applied at the inner strip points  $\xi \equiv (\xi_1, \xi_2)$  along the co-ordinate axis  $0x_k$ , onto the bulk dilatation (the influence functions for the dilatation-  $\Theta^{(k)}(x, \xi)$ ) as well as onto the displacements (the components of the displacement Green's matrix-  $U_i^{(k)}(x, \xi)$  at the points of observation  $x \equiv (x_1, x_2)$  along the co-ordinate axis  $0x_i$ . The formulations and the final Answers to four boundary-value Problem (L2C)s on constructing the influence functions for dilatation and Green's matrices for Lamé's equations in the case of the strip are given here.

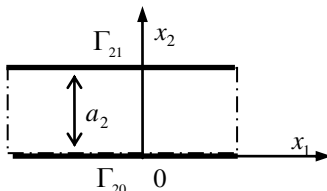


Figure 4: Strip with boundary straight lines  $\Gamma_{20}$  and  $\Gamma_{21}$ .

**Problems (L2C) of First Type. Problems (L2C) 4.1– (L2C) 4.4**

To construct the influence function for the dilatation  $\Theta^{(k)}(x, \xi)$  and for the components of the displacements Green's matrix  $U_i^{(k)}(x, \xi)$  for Lamé's equation for the elastic strip ( $-\infty \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2$ ) under the following locally mixed boundary conditions of a sliding fixation type.

**Problem (L2C) 4. 1**

$$U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = 0, a_2; -\infty \leq x_1 \leq \infty.$$

**The Answer to Problem (L2C) 4.1 for strip** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
 Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

**Problem (L2C) 4. 2**

$$\sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = 0, a_2; -\infty \leq x_1 \leq \infty.$$

**The Answer to Problem (L2C) 4.2 for strip** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
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**Problem (L2C) 4. 3**

$$\left. \begin{array}{l} U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = 0 \\ \sigma_{22}^{(k)} = 0; U_1^{(k)} = 0; x_2 = a_2 \end{array} \right\}, -\infty \leq x_1 \leq \infty.$$

**The Answer to Problem (L2C) 4.3 for strip** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
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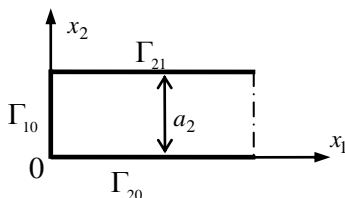
**Problem (L2C) 4. 4**

$$\left. \begin{array}{l} \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = 0 \\ U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = a_2 \end{array} \right\}, -\infty \leq x_1 \leq \infty.$$

**The Answer to Problem (L2C) 4.4 for strip** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
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**(L2C) 5. Half-strip** ( $0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2$ )

Section 5 gives the functions of influence of the unit concentrated body forces  $\int \delta_{ik} \delta(x - \xi) dV(\xi) = \delta_{ik}$ ,  $i, k=1,2$ , applied at the inner points  $\xi \equiv (\xi_1, \xi_2)$  of the half-strip along the co-ordinate axis  $0x_k$ , onto the bulk dilatation ( the influence functions for the dilatation- $\Theta^{(k)}(x, \xi)$ ) as well as onto the displacements (the





components of the displacement Green's matrix  $-U_i^{(k)}(x, \xi)$  at the points of observation  $x \equiv (x_1, x_2)$  along the co-ordinate axis  $0x_i$ . The formulations and the final Answers to 16 boundary-value Problem (L2C)s on constructing the influence functions for dilatation and Green's matrices for Lamé's equations in the case of the half-strip are given there.

Figure 5: Half-strip with boundary half-straight lines  $\Gamma_{20}$  and  $\Gamma_{21}$  a segment of straight line  $\Gamma_{10}$ .

### **Problem (L2C) of First Type. Problems (L2C) 5.1– (L2C) 5.8**

To construct the influence functions for the dilatation  $\Theta^{(k)}(x, \xi)$  and the components of the displacements Green's matrix  $U_i^{(k)}(x, \xi)$  for Lamé's equations for the elastic half-strip ( $0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2$ ) under the following locally mixed boundary-value conditions of a sliding fixation type

#### **Problem (L2C) 5.1**

$$\boxed{U_1^{(k)} = \sigma_{12}^{(k)} = 0; x_1 = 0; 0 \leq x_2 \leq a_2; U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = 0, a_2; 0 \leq x_1 \leq \infty.}$$

**The Answer to Problem (L2C) 5.1 for half-strip** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
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#### **Problem (L2C) 5.2**

$$\boxed{\sigma_{11}^{(k)} = U_2^{(k)} = 0; x_1 = 0; 0 \leq x_2 \leq a_2; \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = 0, a_2; 0 \leq x_1 \leq \infty.}$$

**The Answer to Problem (L2C) 5.2 for half-strip** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
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#### **Problem (L2C) 5.3**

$$\boxed{\sigma_{11}^{(k)} = U_2^{(k)} = 0; x_1 = 0; 0 \leq x_2 \leq a_2; U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = 0, a_2, 0 \leq x_1 \leq \infty.}$$

**The Answer to Problem (L2C) 5.3 for half-strip** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
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**Problem (L2C) 5.4**

$$U_1^{(k)} = \sigma_{12}^{(k)} = 0; x_1 = 0; 0 \leq x_2 \leq a_2; \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = 0, a_2; 0 \leq x_1 \leq \infty.$$

The Answer to Problem (L2C) 5.4 for half-strip (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:

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**Problem (L2C) 5.5**

$$\left. \begin{array}{l} \sigma_{11}^{(k)} = U_2^{(k)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2; \\ U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = 0 \\ \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = a_2 \end{array} \right\}, 0 \leq x_1 \leq \infty.$$

The Answer to Problem (L2C) 5.5 for half-strip (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:

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**Problem (L2C) 5.6**

$$\left. \begin{array}{l} U_1^{(k)} = \sigma_{12}^{(k)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2; \\ U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = 0 \\ \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = a_2 \end{array} \right\}, 0 \leq x_1 \leq \infty.$$

The Answer to Problem (L2C) 5.6 for half-strip (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:

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**Problem (L2C) 5.7**

$$\left. \begin{array}{l} \sigma_{11}^{(k)} = U_2^{(k)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2; \\ \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = a_2 \\ U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = 0 \end{array} \right\}, 0 \leq x_1 \leq \infty.$$

The Answer to Problem (L2C) 5.7 for half-strip (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:

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**Problem (L2C) 5.8**

$$\left. \begin{array}{l} U_1^{(k)} = \sigma_{12}^{(k)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2; \\ \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = a_2 \\ U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = 0 \end{array} \right\}, 0 \leq x_1 \leq \infty.$$

**The Answer to Problem (L2C) 5.8 for half-strip** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
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## Problems (L2C) of Second Type. Problems (L2C) 5.9– (L2C) 5.12

To construct the influence functions for the dilatation  $\Theta^{(k)}(x, \xi)$  and the components of the displacements Green's matrix  $U_i^{(k)}(x, \xi)$  for Lamé's equation for the elastic half-strip  $(0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2)$  under the following locally mixed boundary conditions of rigid and sliding fixation type.

### Problem (L2C) 5.9

$$U_1^{(k)} = U_2^{(k)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2; U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = 0, a_2, 0 \leq x_1 \leq \infty.$$

**The Answer to Problem (L2C) 5.9 for half-strip** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
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### Problem (L2C) 5.10

$$U_1^{(k)} = U_2^{(k)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2; \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = 0, a_2; 0 \leq x_1 \leq \infty.$$

**The Answer to Problem (L2C) 5.10 for half-strip** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

### Problem (L2C) 5.11

$$U_1^{(k)} = U_2^{(k)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2 \left. \begin{array}{l} U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = 0 \\ \sigma_{22} = U_1^{(k)} = 0; x_2 = a_2. \end{array} \right\} 0 \leq x_1 \leq \infty.$$

**The Answer to Problem (L2C) 5.11 for half-strip** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
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**Problem (L2C) 5.12**

$$\left. \begin{aligned} U_1^{(k)} = U_2^{(k)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2; \quad \sigma_{22} = U_1^{(k)} = 0; x_2 = 0 \\ U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = a_2 \end{aligned} \right\}, 0 \leq x_1 \leq \infty.$$

The Answer to Problem (L2C) 5.12 for half-strip (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
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**Problems (L2C) of Third Type. Problems (L2C) 5.13– (L2C) 5.16**

To construct the influence functions for the dilatation  $\Theta^{(k)}(x, \xi)$  and the components of the displacements Green's matrix  $U_i^{(k)}(x, \xi)$  for Lamé's equation for the elastic half-strip ( $0 \leq x_1 \leq \infty, 0 \leq x_2 \leq a_2$ ) under the following mixed boundary-value conditions of a type of free edge and sliding fixations on the parallel sides

**Problem (L2C) 5.13**

$$\left. \begin{aligned} \sigma_{11}^{(k)} = \sigma_{12}^{(k)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2; \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = 0, a_2, 0 \leq x_1 \leq \infty \end{aligned} \right\}.$$

The Answer to Problem (L2C) 5.13 for half-strip (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
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**Problem (L2C) 5.14**

$$\left. \begin{aligned} \sigma_{11}^{(k)} = \sigma_{12}^{(k)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2; U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = 0, a_2, 0 \leq x_1 \leq \infty \end{aligned} \right\}.$$

The Answer to Problem (L2C) 5.14 for half-strip (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

**Problem (L2C) 5.15**

$$\left. \begin{aligned} \sigma_{11}^{(k)} = \sigma_{12}^{(k)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2; \quad U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = 0 \\ \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = a_2 \end{aligned} \right\}, 0 \leq x_1 \leq \infty.$$

The Answer to Problem (L2C) 5.15 for half-strip (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:

**Problem (L2C) 5.16**

$$\left. \begin{aligned} \sigma_{11}^{(k)} = \sigma_{12}^{(k)} = 0; x_1 = 0, 0 \leq x_2 \leq a_2; \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = 0 \\ U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = a_2 \end{aligned} \right\}, 0 \leq x_1 \leq \infty .$$

**The Answer to Problem (L2C) 5.16 for half-strip** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book: Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

**(L2C) 6. Rectangle** ( $0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2$ )

Section 6 gives the influence of the unit concentrated body forces  $\int_V \delta_{ik} \delta(x - \xi) dV(\xi) = \delta_{ik}$ ,  $i, k=1, 2$ , applied at the inner rectangle points  $\xi \equiv (\xi_1, \xi_2)$  along co-ordinate axis  $0x_k$ , onto the bulk dilatation (the influence functions for the dilatation  $-\Theta^{(k)}(x, \xi)$ ) as well as onto the displacements (the components of the displacements Green's matrix  $-U_i^{(k)}(x, \xi)$ ) at the points of observation  $x \equiv (x_1, x_2)$  along co-ordinate axis  $0x_i$ . The formulations and the final Answers to 14 boundary-value Problem (L2C)s on constructing the influence functions for dilatation and Green's matrices for Lamé's equations in the case of the rectangle are given there.

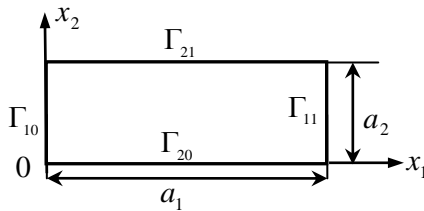


Figure 6: rectangle with boundary segments of straight lines  $\Gamma_{10}, \Gamma_{11}$  and  $\Gamma_{20}, \Gamma_{21}$ .

**Problems (L2C) of First Type. Problems (L2C) 6.1– (L2C) 6.14**

To construct the influence functions for the dilatation  $-\Theta^{(k)}(x, \xi)$  and for the components of the displacements Green's matrix  $U_i^{(k)}(x, \xi)$  for Lamé's equation

in the case of elastic rectangle  $(0 \leq x_1 \leq a_1, 0 \leq x_2 \leq a_2)$  under the following locally mixed boundary conditions of a type of sliding fixations:

**Problem (L2C) 6.1**

$$U_1^{(k)} = \sigma_{12}^{(k)} = 0; x_1 = 0, a_1 \quad 0 \leq x_2 \leq a_2; U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = 0, a_2, \quad 0 \leq x_1 \leq a_1$$

**The Answer to Problem (L2C) 6.1 for rectangle** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:

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**Problem (L2C) 6.2**

$$\sigma_{11}^{(k)} = U_2^{(k)} = 0; x_1 = 0, a_1, \quad 0 \leq x_2 \leq a_2; \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = 0, a_2, \quad 0 \leq x_1 \leq a_1.$$

**The Answer to Problem (L2C) 6.2 for rectangle** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:

Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

**Problem (L2C) 6.3**

$$\left. \begin{array}{l} \sigma_{11}^{(k)} = U_2^{(k)} = 0; x_1 = 0, \\ U_1^{(k)} = \sigma_{12}^{(k)} = 0; x_1 = a_1 \end{array} \right\} 0 \leq x_2 \leq a_2; U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = 0, a_2, \quad 0 \leq x_1 \leq a_1.$$

**The Answer to Problem (L2C) 6.3 for rectangle** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:

Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

**Problem (L2C) 6.4**

$$U_1^{(k)} = \sigma_{12}^{(k)} = 0; x_1 = 0, a_1, \quad 0 \leq x_2 \leq a_2; \left. \begin{array}{l} \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = 0, \\ U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = a_2. \end{array} \right\} 0 \leq x_1 \leq a_1.$$

**The Answer to Problem (L2C) 6.4 for rectangle** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:

Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

**Problem (L2C) 6.5**

$$\left. \begin{array}{l} \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = 0, a_2, 0 \leq x_1 \leq a_1; \\ U_1^{(k)} = \sigma_{12}^{(k)} = 0; x_1 = a_1 \\ \sigma_{11}^{(k)} = U_1^{(k)} = 0; x_1 = 0 \end{array} \right\}, 0 \leq x_2 \leq a_2.$$

The Answer to Problem (L2C) 6.5 for **rectangle** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

**Problem (L2C) 6.6**

$$\left. \begin{array}{l} \sigma_{11}^{(k)} = U_2^{(k)} = 0; x_1 = 0 \\ x_1 = a_1 \end{array} \right\}, 0 \leq x_2 \leq a_2; \left. \begin{array}{l} \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = 0. \\ U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = a_2. \end{array} \right\}, 0 \leq x_1 \leq a_1.$$

The Answer to Problem (L2C) 6.6 for **rectangle** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

**Problem (L2C) 6.7**

$$\left. \begin{array}{l} \sigma_{11}^{(k)} = U_2^{(k)} = 0; x_1 = a_1 \\ U_1^{(k)} = \sigma_{12}^{(k)} = 0; x_1 = 0 \end{array} \right\}, 0 \leq x_2 \leq a_2; \left. \begin{array}{l} \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = 0 \\ U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = a_2 \end{array} \right\}, 0 \leq x_1 \leq a_1.$$

The Answer to Problem (L2C) 6.7 for **rectangle** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

**Problem (L2C) 6.8**

$$\left. \begin{array}{l} \sigma_{11}^{(k)} = U_2^{(k)} = 0; x_1 = 0 \\ U_1^{(k)} = \sigma_{12}^{(k)} = 0; x_1 = a_1 \end{array} \right\}, 0 \leq x_2 \leq a_2; \left. \begin{array}{l} U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = 0 \\ \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = a_2 \end{array} \right\}, 0 \leq x_1 \leq a_1.$$

The Answer to Problem (L2C) 6.8 for **rectangle** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
Seremet V.D. Handbook of Green's functions and matrices - WIT press, Southampton and Boston, UK&USA, 2003, Book 304 p. + CD ROM, 232 p. (in English)

**Problem (L2C) 6.9**

$$\left. \begin{array}{l} \sigma_{11}^{(k)} = U_2^{(k)} = 0; x_1 = 0 \\ U_1^{(k)} = \sigma_{12}^{(k)} = 0; x_1 = a_1 \end{array} \right\} 0 \leq x_2 \leq a_2; \quad \left. \begin{array}{l} \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = 0 \\ U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = a_2 \end{array} \right\} 0 \leq x_1 \leq a_1.$$

The Answer to Problem (L2C) 6.9 for **rectangle** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
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**Problem (L2C) 6.10**

$$\left. \begin{array}{l} U_1^{(k)} = \sigma_{12}^{(k)} = 0; x_1 = 0, a_1, 0 \leq x_2 \leq a_2; \\ \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = a_2 \end{array} \right\} 0 \leq x_1 \leq a_1, \quad \left. \begin{array}{l} U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = 0. \\ \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = a_2 \end{array} \right\} 0 \leq x_1 \leq a_1.$$

The Answer to Problem (L2C) 6.10 for **rectangle** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
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**Problem (L2C) 6.11**

$$\left. \begin{array}{l} \sigma_{11}^{(k)} = U_2^{(k)} = 0; x_1 = 0, a_1, 0 \leq x_2 \leq a_2; \\ \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = a_2 \end{array} \right\} 0 \leq x_1 \leq a_1, \quad \left. \begin{array}{l} U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = 0. \\ \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = a_2 \end{array} \right\} 0 \leq x_1 \leq a_1.$$

The Answer to Problem (L2C) 6.11 for **rectangle** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
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**Problem (L2C) 6.12**

$$\left. \begin{array}{l} \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = 0, a_2, 0 \leq x_1 \leq a_1; \\ \sigma_{11}^{(k)} = U_2^{(k)} = 0; x_1 = a_1 \end{array} \right\} 0 \leq x_1 \leq a_1, \quad \left. \begin{array}{l} U_1^{(k)} = \sigma_{12}^{(k)} = 0; x_1 = 0 \\ \sigma_{11}^{(k)} = U_2^{(k)} = 0; x_1 = a_1 \end{array} \right\} 0 \leq x_1 \leq a_1.$$

The Answer to Problem (L2C) 6.12 for **rectangle** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
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**Problem (L2C) 6.13**

$$\left. \begin{array}{l} U_1^{(k)} = \sigma_{12}^{(k)} = 0; x_1 = 0 \\ \sigma_{11}^{(k)} = U_2^{(k)} = 0; x_1 = a_1 \end{array} \right\}, 0 \leq x_2 \leq a_2; \left. \begin{array}{l} U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = 0. \\ \sigma_{22}^{(k)} = U_1^{(k)} = 0; x_2 = a_2. \end{array} \right\}, 0 \leq x_1 \leq a_1 .$$

The Answer to Problem (L2C) 6.13 for **rectangle** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
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**Problem (L2C) 6.14**

$$\left. \begin{array}{l} U_1^{(k)} = \sigma_{12}^{(k)} = 0; x_1 = 0 \\ \sigma_{11}^{(k)} = U_2^{(k)} = 0; x_1 = a_1 \end{array} \right\}, 0 \leq x_2 \leq a_2; \left. \begin{array}{l} U_2^{(k)} = \sigma_{21}^{(k)} = 0; x_2 = 0, a_2, \\ 0 \leq x_1 \leq a_1 . \end{array} \right\}$$

The Answer to Problem (L2C) 6.14 for **rectangle** (Green's tensor for Lamé's equation in Cartesian coordinates) can be found in the book:  
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